



# A Collider Roadmap to Composite Higgs Models

Giacomo Cacciapaglia  
LPTHE Jussieu, Sorbonne U., France

RTG 2994 Inauguration Workshop  
Würzburg  
18-03-2025



# Motivation

- Composite models 'solve' the Hierarchy problem...
- with new scale in the multi-TeV!

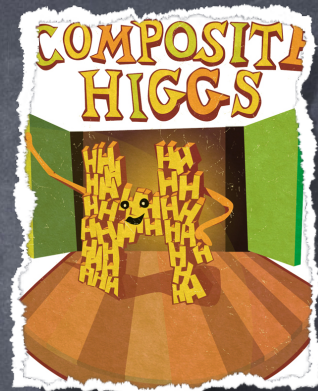


multi-TeV  
mountain

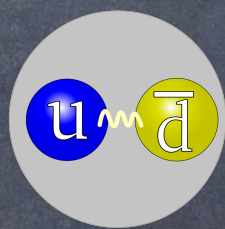
- What are we looking for?
  - > Precision EW + Higgs observables
  - > light composite scalars
  - > multi-TeV resonances (top partners, pNGBs, spin-1)



# Composite Higgs models 101



- Symmetry broken by a condensate (of TC-fermions)
- Higgs and longitudinal Z/W emerge as mesons (pions)



Scales:

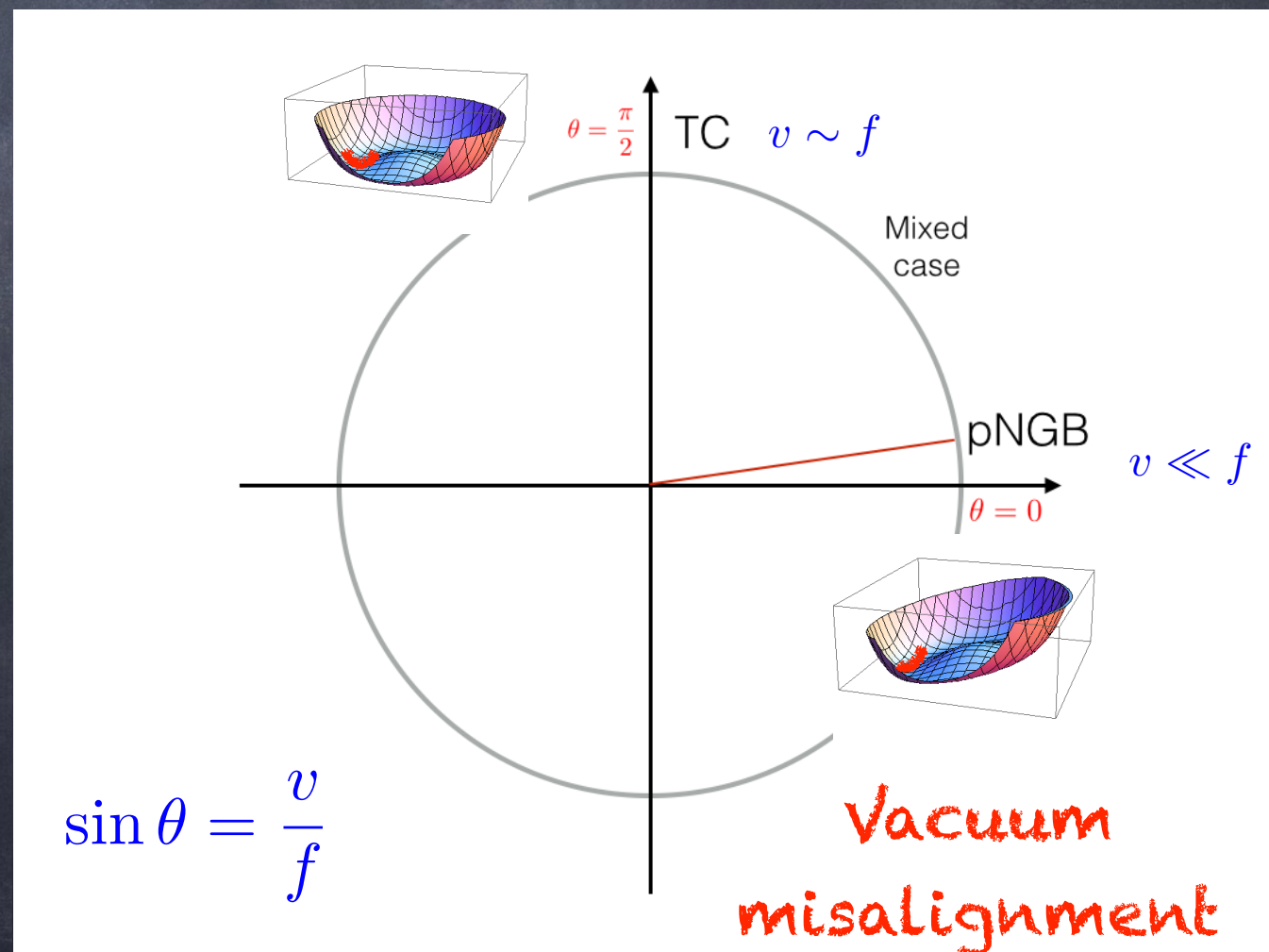
$f$  : Higgs decay constant

$v$  : EW scale

$$m_\rho \sim 4\pi f$$

EWPTs + Higgs coupl. limit:

$$f \gtrsim 4v \sim 1 \text{ TeV}$$







# Composite Higgs models 101

How can Light states emerge?

Top loops



Gauge loops



TC-fermion masses



$\phi$	$\sim y_t^2 f^2$	$\sim g^2 f^2$	$\sim m_\psi f$
$h$ ( $h$ massless for vanishing $v$ )	$\sim y_t^2 f^2 s_\theta^2 = y_t^2 v^2$	$\sim g^2 f^2 s_\theta^2 = g^2 v^2$	X
$a$	X	X	$\sim m_\psi f$ This can be small!



# The partial compositeness paradigm

Kaplan Nucl.Phys. B365 (1991) 259

$$[\mathcal{O}_H = \psi\psi] \quad \frac{1}{\Lambda_{\text{fl.}}^{d-1}} \mathcal{O}_H q_L^c q_R \quad \Delta m_H^2 \sim \left( \frac{4\pi f}{\Lambda_{\text{fl.}}} \right)^{d-4} f^2 \quad \text{Both irrelevant if}$$

we assume:  $d_H > 1$   $d_{H^2} > 4$

Let's postulate the existence of fermionic operators:

$$[F = \psi\psi\psi] \quad \frac{1}{\Lambda_{\text{fl.}}^{d_F-5/2}} (\tilde{y}_L q_L \mathcal{F}_L + \tilde{y}_R q_R \mathcal{F}_R)$$

This dimension is not related to the Higgs!



$$f(y_L q_L Q_L + y_R q_R Q_R) \quad \text{with} \quad y_{L/R} f \sim \left( \frac{4\pi f}{\Lambda_{\text{fl.}}} \right)^{d_F-5/2} 4\pi f$$



# Sequestering QCD in Partial compositeness

$\mathcal{G}_{TC}$  : rep  $R$

$\psi$

rep  $R'$

$\chi$

G.Ferretti, D.Karateev  
1312.5330, 1604.06467

$T = \psi\psi\chi$  or  $\psi\chi\chi$

SM : EW

colour + hypercharge

global :  $\langle \psi\psi \rangle \neq 0$



pNGB Higgs  
DM?

a)  $\langle \chi\chi \rangle \neq 0$

coloured pNGBs  
di-boson

b)  $\langle \chi\chi \rangle = 0$

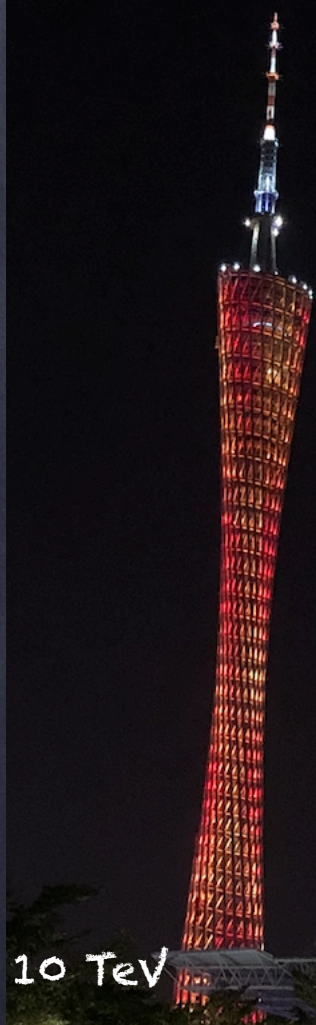
light top partners  
from 1-Hooft anomaly  
conditions?



# Composite models at various scales

G.C., S.Vatani, C.Zhang  
1911.05454, 2005.12302

Planck scale



10 TeV

Condensation scale  $\Lambda_{TC} \sim 4\pi f$

Usual low energy description  
of composite Higgs models

One of Ferretti  
models

Standard Model

100 GeV



# Composite models at various scales

G.C., S.Vatani, C.Zhang  
1911.05454, 2005.12302

Planck scale

HC and SM gauge groups  
partially unified

Symmetry breaking by scalars

4-fermion Ops  
generated!

Conformal window  
(large scaling dimensions)

One of Ferretti  
models +  
additional fermions

10 TeV

Condensation scale  $\Lambda_{TC} \sim 4\pi f$

Usual low energy description  
of composite Higgs models

One of Ferretti  
models

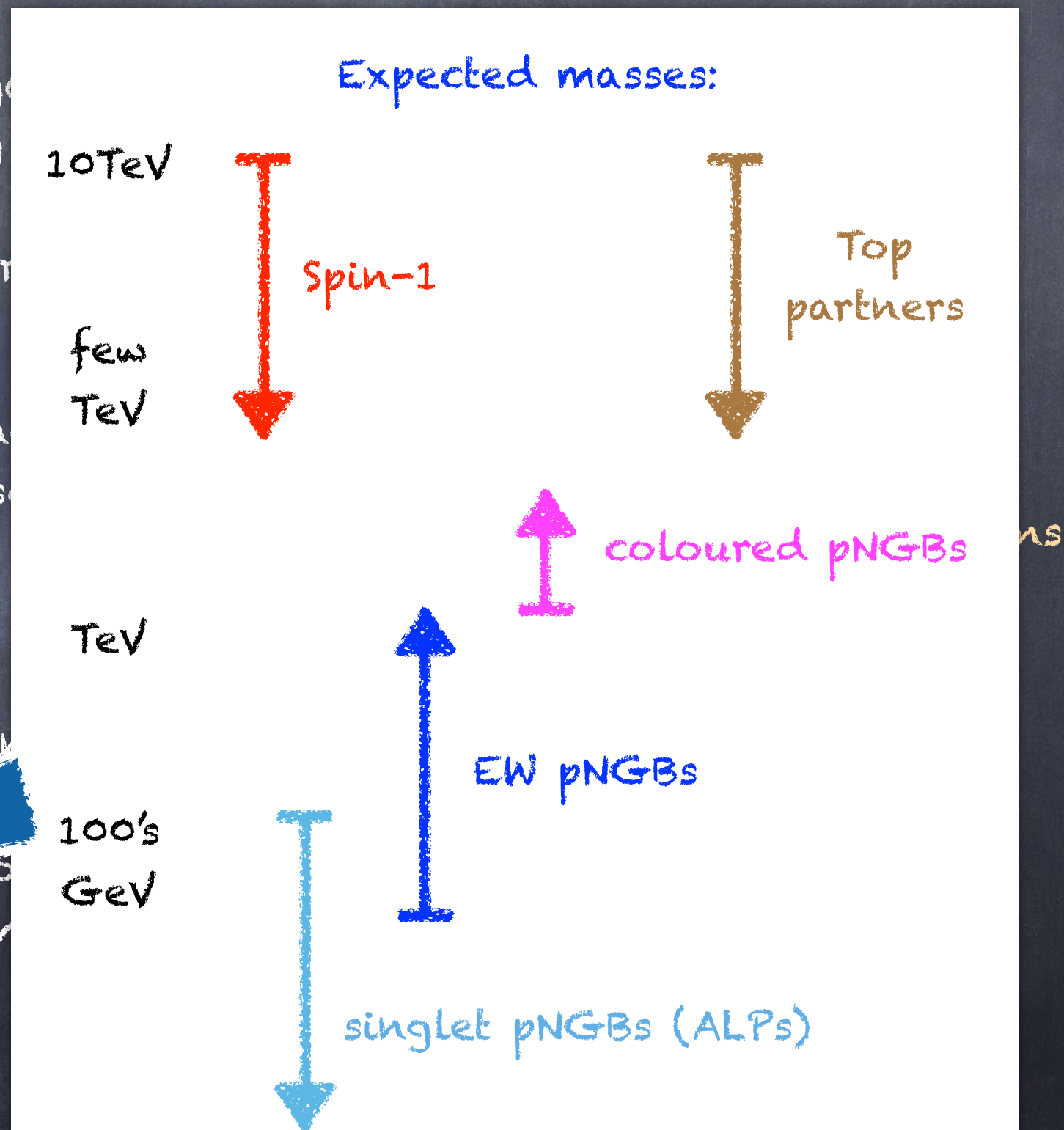
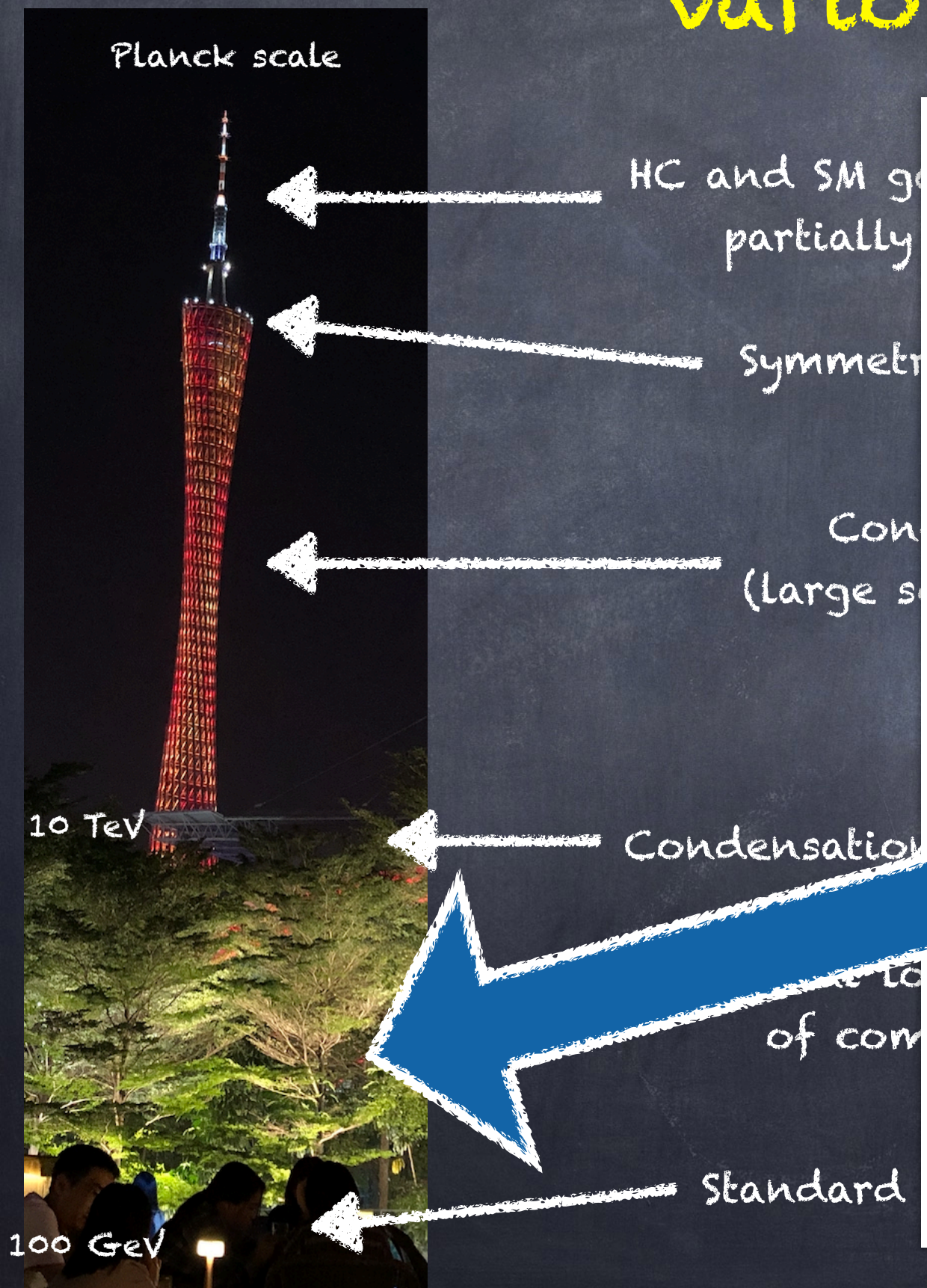
Standard Model

100 GeV





# Composite models at various scales





# Roadmap to Higgs compositeness

- The HL-LHC will leave an important legacy, but NOT covering the whole interesting parameter space! (i.e. 10 TeV is the target)
- A Tera-Z run will fully test the presence of a light composite ALP  $\rightarrow$  well beyond the 10 TeV mark
- Case 1 : discovery + EWPTs can fix the scale
- Case 2 : non-discovery + EWPTs
- In both cases, the results will strongly constraint the model building, providing testable predictions for a high energy pp collider, which will fully cover the scenario.

\* Not including flavour, cosmology, ...



# The LHC legacy

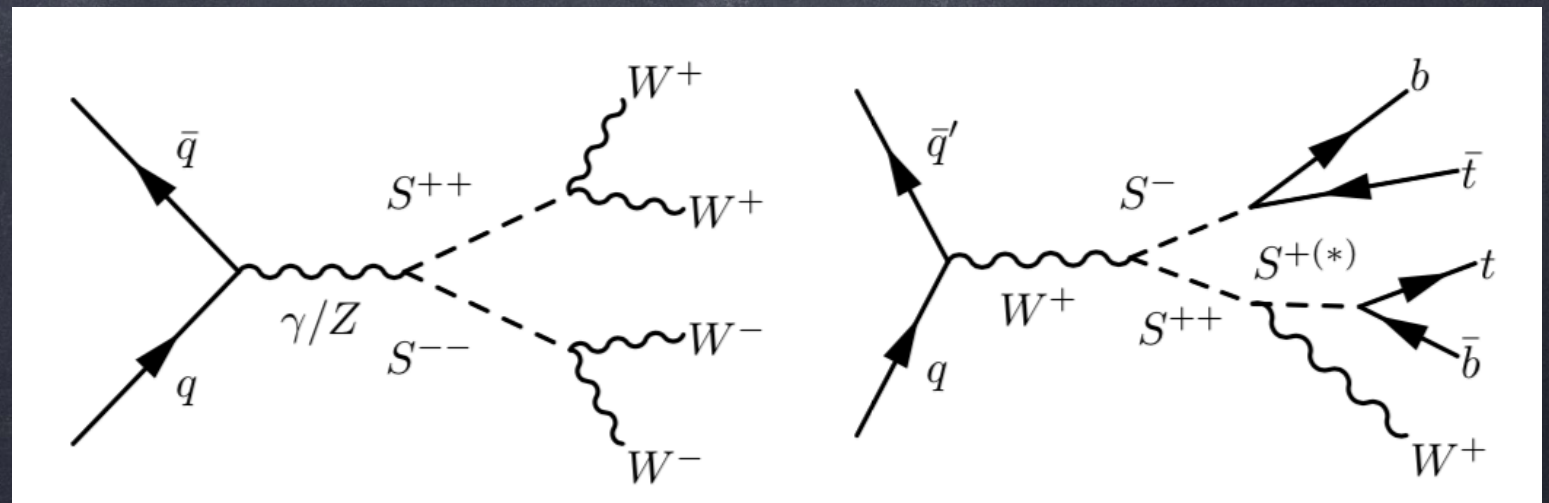
- The Higgs - couplings
- EW-charged scalars (few 100's GeV)
- Singlets (ALPs) that couple to gluons
- Spin-1 resonances (EW)
- Coloured states (QCD)



# EW pNGB direct production

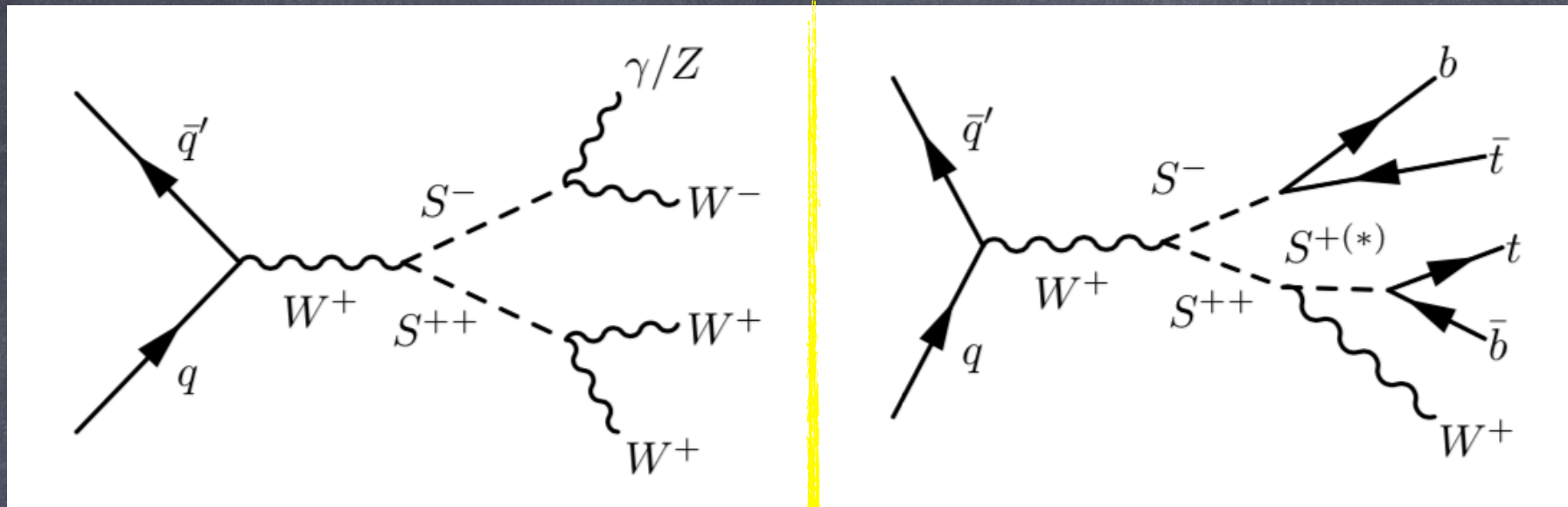
G.C., W.Porod, T.Flacke, L.Schwarze  
2210.01826

- Dominantly pair-produced (no VEVs except for the doublet)
- Couplings to two EW gauge bosons via topological anomalies, not VEVs  $\rightarrow$  photons are present!!!
- Couplings to two fermions via partial compositeness
- Few dedicated direct searches (WWWW and WWWZ via doubly-charged scalar)





# EW pNGB direct production



W. Porod et al.  
2210.01826

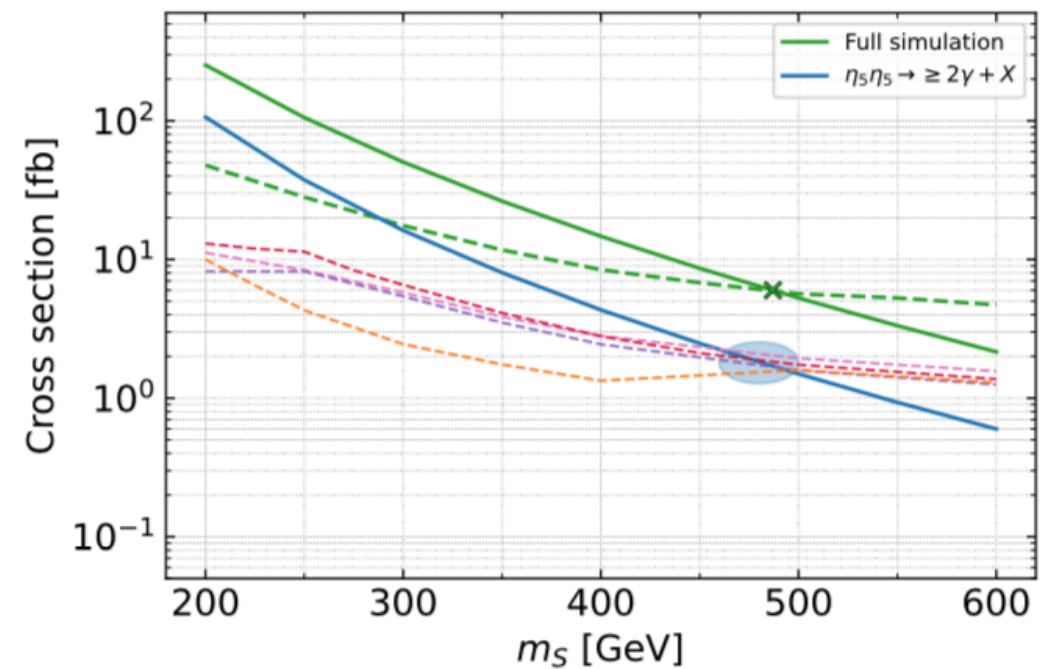
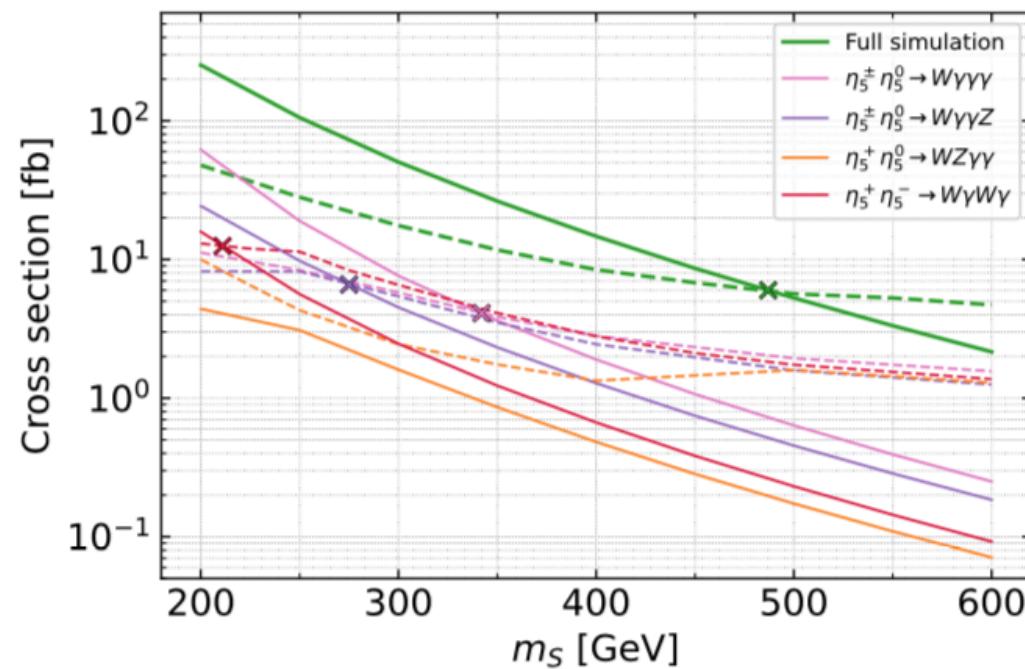
- Decays to two GBs from anomaly
- Small couplings
- Cascade decays can be competitive
- Photon-rich final states!



# SU(5)/SO(5) benchmark

W. Porod et al.

2210.01826



- Run all searches in MadAnalysis, Checkmate and Contur on all di-scalar pair production channels.
- Best limits from multi-photon searches (ATLAS generic analysis)
- Many channels contribute to the same signal region!



# SU(5)/SO(5) benchmark

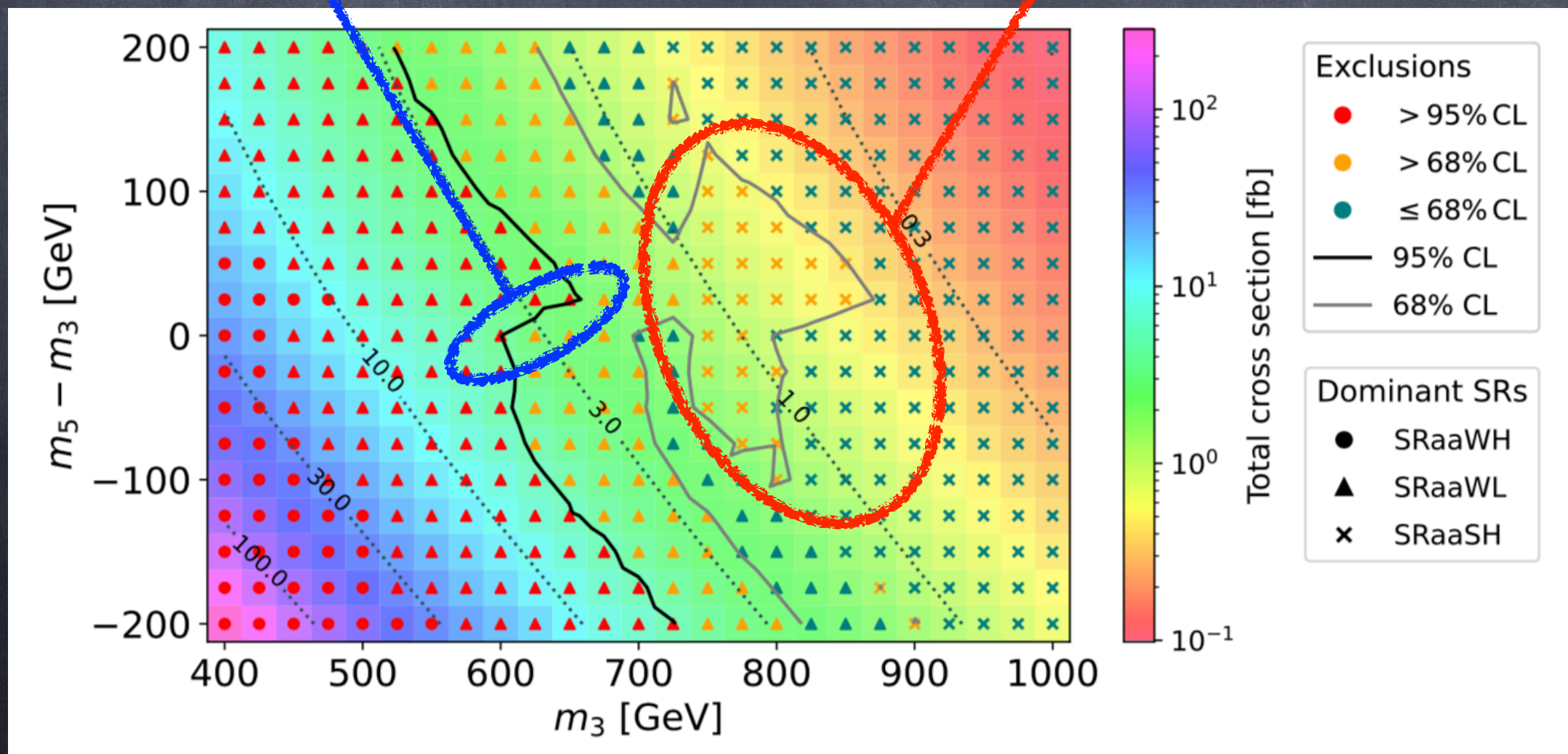
W.Porod et al.

2210.01826

## Exclusion from multi-photon search

$S^{++}$  cascade decays

Change in dominant SR





# The QCD sector

(Above the TeV scale)

- Coloured pNGBs
- Top partners
- Spin-1 resonances



# The models

EW \ QCD	SU(4)/Sp(4)	SU(5)/SO(5)	SU(4) <sup>2</sup> /SU(4)
SU(6)/Sp(6)		M5 ( $\psi\chi\chi$ )	
SU(6)/SO(6)	M8-9 ( $\psi\psi\chi$ )	M3-4 ( $\psi\psi\chi$ ) M1-2 ( $\psi\chi\chi$ )	M10-11 ( $\psi\psi\chi$ )
SU(3) <sup>2</sup> /SU(3)		M6-7 ( $\psi\chi\chi$ )	M12 ( $\psi\psi\chi$ )

7 classes  
of models!

Focusing on QCD-charged states:

	Models	$\chi (R, Y, B)$	$\pi$	$\mathcal{V}^\mu$	$\mathcal{A}^\mu$	$\Psi$	di-quark
C1	M1-2	$(R, -\frac{1}{3}, \frac{1}{6})$	$8_0, \text{Red } 6_{-2/3}$	$8_0, 1_0, \text{Red } 3_{2/3}$	$8_0, \text{Red } 6_{-2/3}$	$8, 1, \text{Red } 3, \text{Red } 6$	none
C2	M3-4, M8-11	$(R, \frac{2}{3}, \frac{1}{3})$	$8_0, \text{Blue } 6_{4/3}$	$8_0, 1_0, \text{Blue } 3_{-4/3}$	$8_0, \text{Blue } 6_{4/3}$	$\text{Red } 3$	$\pi_6, \mathcal{V}_3^\mu, \mathcal{A}_6^\mu$
C3	M5	$(Pr, -\frac{1}{3}, \frac{1}{6})$	$8_0, \text{Red } 3_{2/3}$	$8_0, 1_0, \text{Red } 6_{-2/3}$	$8_0, \text{Red } 3_{2/3}$	$8, 1, \text{Red } 3, \text{Red } 6$	none
C4	M6-7	$(C, -\frac{1}{3}, \frac{1}{6})$	$8_0$	$8_0, 1_0$	$8_0$	$8, 1, \text{Red } 3, \text{Red } 6$	none
C5	M12	$(C, \frac{2}{3}, \frac{1}{3})$	$8_0$	$8_0, 1_0$	$8_0$	$\text{Red } 3$	none

Red:  $B = 1/3$

Blue:  $B = 2/3$



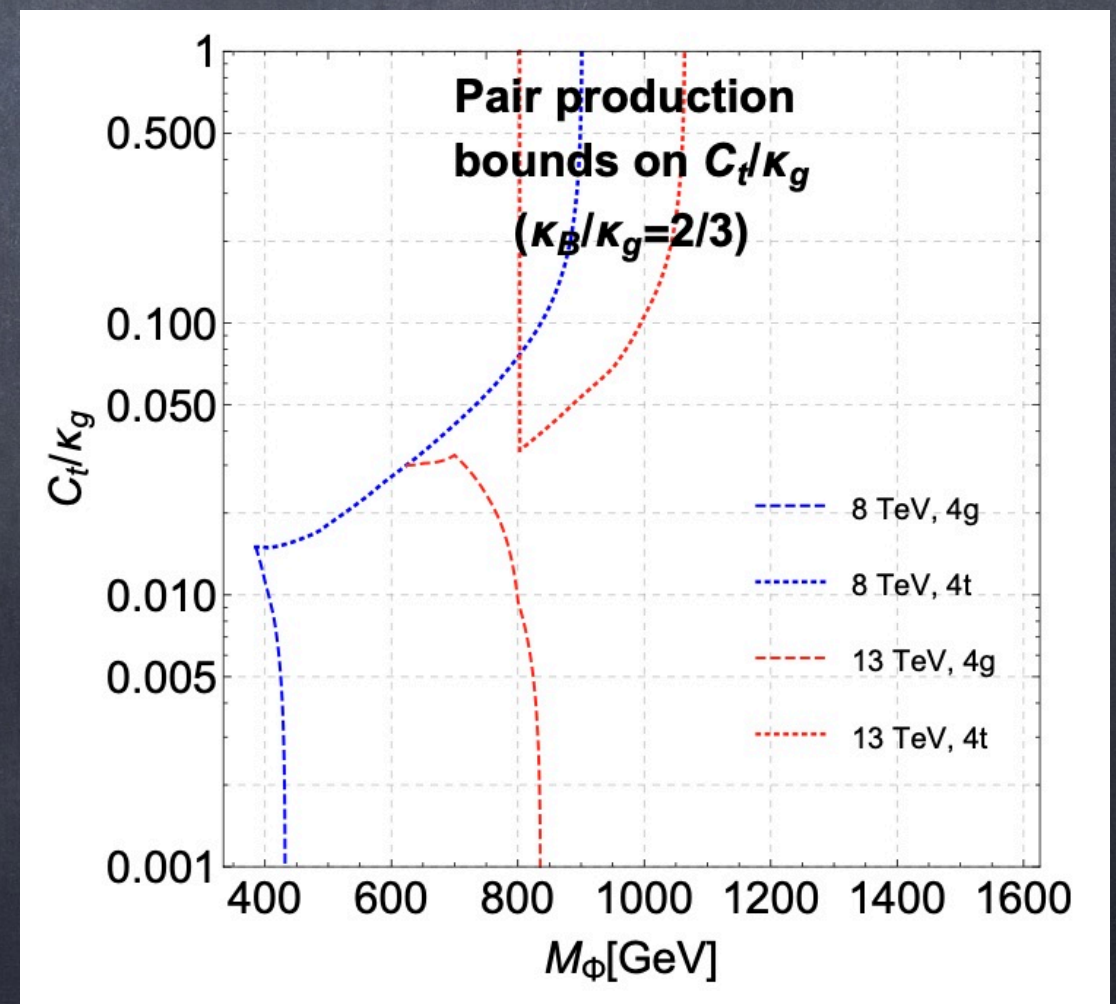
# Coloured pNGBs

- They are always present in models.
- They are relatively light (TeV scale)

C1 :  $\pi_8 \rightarrow t\bar{t}, gg; \pi_6 \rightarrow b\bar{b},$   
 C2 :  $\pi_8 \rightarrow t\bar{t}, gg; \pi_6 \rightarrow t\bar{t},$   
 C3 :  $\pi_8 \rightarrow t\bar{t}, gg; \pi_3 \rightarrow \bar{b}s \text{ or } t\bar{\nu}, b\tau^+,$   
 C4-5 :  $\pi_8 \rightarrow t\bar{t}, gg.$

2002.01474

Octet  $\left\{ \begin{array}{l} \pi_8 \rightarrow t\bar{t} \quad (\text{squon-like}) \\ \pi_8 \rightarrow gg, g\gamma \end{array} \right.$   
 Triplet  $\left\{ \begin{array}{l} \pi_3 \rightarrow b\bar{s} \\ \pi_3 \rightarrow t\chi \end{array} \right. \quad (\text{stop-like})$   
 Sextet  $\left\{ \begin{array}{l} \pi_6 \rightarrow t\bar{t} \\ \pi_6 \rightarrow b\bar{b} \end{array} \right.$

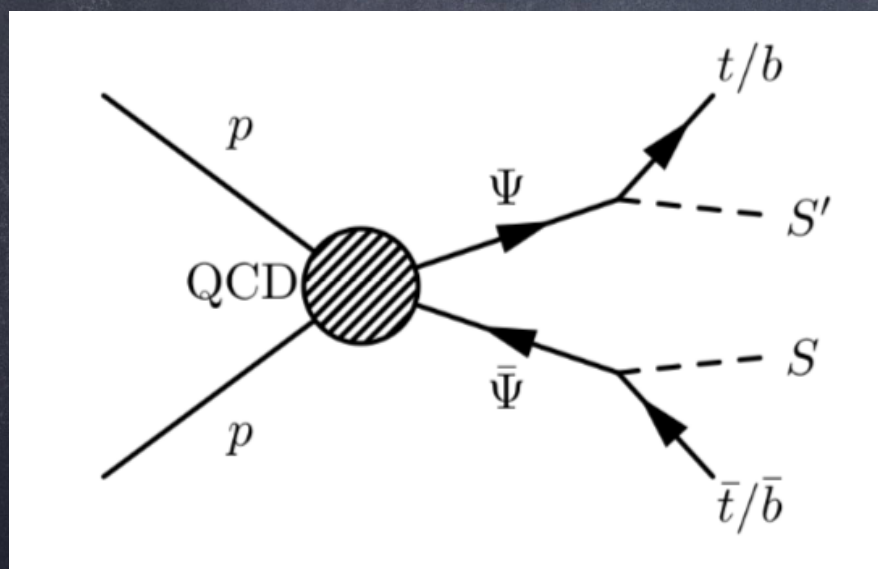




# Top partner pheno revisited

A.Banerjee et al  
2203.0727 (Snowmass LOI)

- Dedicated searches in SM final states:  $tZ$ ,  $bW$ ,  $tH$ ...
- pNGBs lighter than the top partners are to be expected in all composite models



The  $S$  decays are model-dependent, but they can be classified:

$$\begin{aligned} S_i^{++} &\rightarrow W^+ W^+ \\ S_i^+ &\rightarrow W^+ \gamma, W^+ Z \\ S_i^0 &\rightarrow W^+ W^-, \gamma\gamma, \gamma Z, ZZ. \end{aligned}$$

Calculable ratios (from anomalies) and always present for all models.

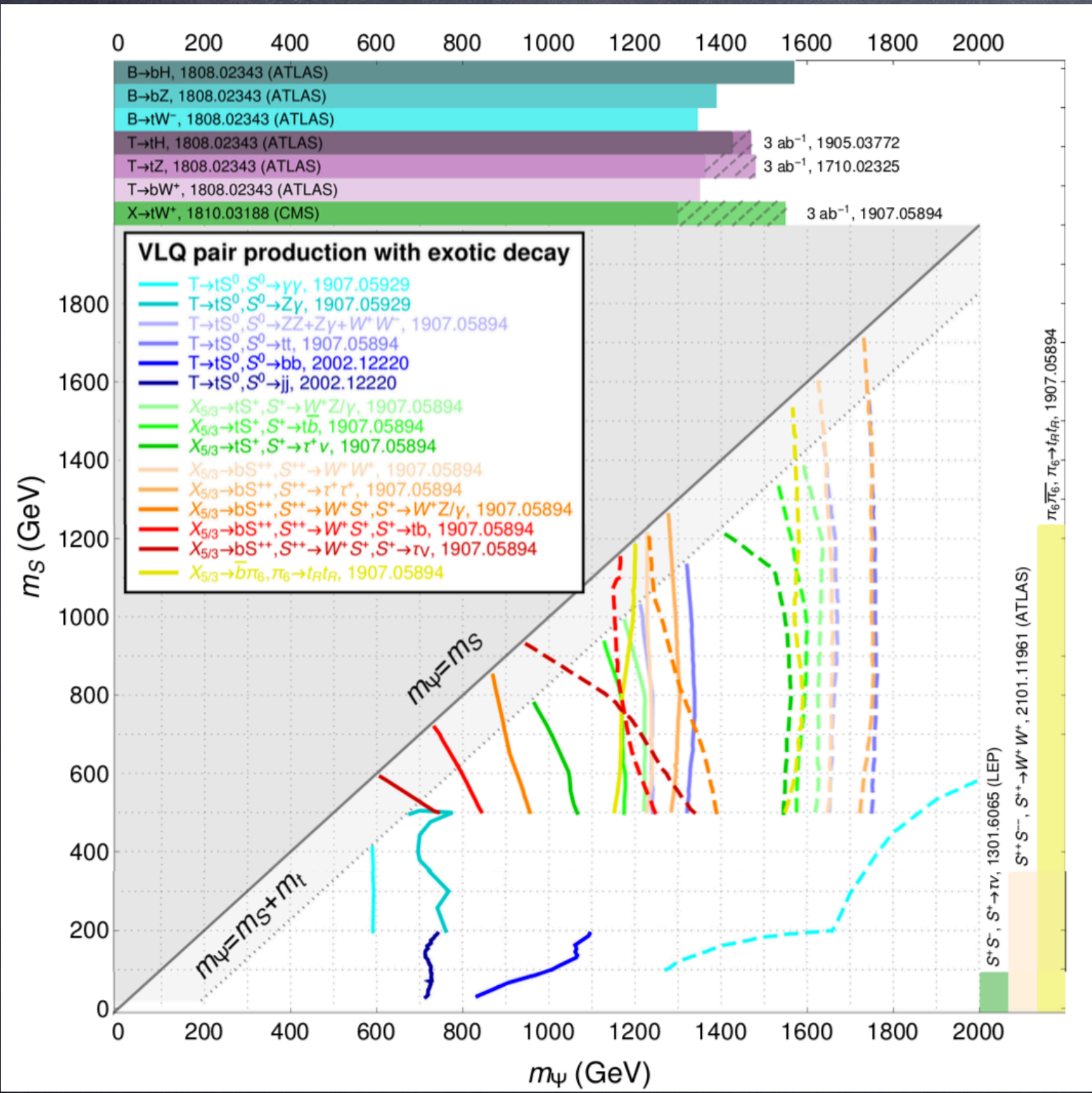
$$\begin{aligned} S^{++} &\rightarrow W^+ t \bar{b}, \\ S^+ &\rightarrow t \bar{b}, \\ S^0 &\rightarrow t \bar{t}, b \bar{b}. \end{aligned}$$

Dominant, if present for the specific  $S$ .



# Common exotic top partner decays

A. Banerjee et al  
2203.0727 (Snowmass LOI)



- Dedicated searches may be useful to push up the limits.
- Projections for FCC-hh are needed...
- in combination with scalar direct production.



# Exotic top partners

	Models	$\chi (R, Y, B)$	$\pi$	$\nu^\mu$	$\mathcal{A}^\mu$	$\Psi$	di-quark
C1	M1-2	$(R, -\frac{1}{3}, \frac{1}{6})$	$8_0, \mathbf{6}_{-2/3}$	$8_0, 1_0, \mathbf{3}_{2/3}$	$8_0, \mathbf{6}_{-2/3}$	$8, 1, \mathbf{3}, \mathbf{6}$	none
C2	M3-4, M8-11	$(R, \frac{2}{3}, \frac{1}{3})$	$8_0, \mathbf{6}_{4/3}$	$8_0, 1_0, \mathbf{3}_{-4/3}$	$8_0, \mathbf{6}_{4/3}$	$\mathbf{3}$	$\pi_6, \mathcal{V}_3^\mu, \mathcal{A}_6^\mu$
C3	M5	$(Pr, -\frac{1}{3}, \frac{1}{6})$	$8_0, \mathbf{3}_{2/3}$	$8_0, 1_0, \mathbf{6}_{-2/3}$	$8_0, \mathbf{3}_{2/3}$	$8, 1, \mathbf{3}, \mathbf{6}$	none
C4	M6-7	$(C, -\frac{1}{3}, \frac{1}{6})$	$8_0$	$8_0, 1_0$	$8_0$	$8, 1, \mathbf{3}, \mathbf{6}$	none
C5	M12	$(C, \frac{2}{3}, \frac{1}{3})$	$8_0$	$8_0, 1_0$	$8_0$	$\mathbf{3}$	none

Models in C1, C3 and C4 contain top-partners as octet and sextet!

$\psi\chi\chi$  types

Larger production than the triplets!



# Exotic top partners

G.C., T.Flacke, M.Kunkel, W.Porod  
2112.00019

- A specific model: MS of Ferretti's classification

## Hyper-fermions

	$\text{Sp}(2N_c)$	$\text{SU}(3)_c$	$\text{SU}(2)_L$	$\text{U}(1)_Y$	$\text{SU}(5)$	$\text{SU}(6)$	$\text{U}(1)$	
$\psi_{1,2}$	$\begin{array}{ c } \hline \square \\ \hline \end{array}$	<b>1</b>	<b>2</b>	$1/2$	<b>5</b>	<b>1</b>	$-\frac{3q_\chi}{5(N_c-1)}$	
$\psi_{3,4}$	$\begin{array}{ c } \hline \square \\ \hline \end{array}$	<b>1</b>	<b>2</b>	$-1/2$				
$\psi_5$	$\begin{array}{ c } \hline \square \\ \hline \end{array}$	<b>1</b>	<b>1</b>	$0$				
$\chi_1$	$\square$	<b>3</b>	<b>1</b>	$-x$	<b>1</b>	<b>6</b>	$q_\chi$	
$\chi_2$								
$\chi_3$								
$\chi_4$	$\square$	$\bar{\mathbf{3}}$	<b>1</b>	$x$				
$\chi_5$								
$\chi_6$								

$$x = -1/3$$

## Chimera Baryons (top partners)

	$\text{SU}(5) \times \text{SU}(6)$	$\text{SO}(5) \times \text{Sp}(6)$	names
$\psi\chi\chi$	<b>(5, 15)</b>	<b>(5, 14)</b>	$\mathcal{B}_{14}^1$
		<b>+(5, 1)</b>	$\mathcal{B}_1^1$
	<b>(5, 21)</b>	<b>(5, 21)</b>	$\mathcal{B}_{21}^1$
$\psi\bar{\chi}\bar{\chi}$	<b>(5, <math>\bar{15}</math>)</b>	<b>(5, 14)</b>	$\mathcal{B}_{14}^2$
		<b>+(5, 1)</b>	$\mathcal{B}_1^2$
	<b>(5, <math>\bar{21}</math>)</b>	<b>(5, 21)</b>	$\mathcal{B}_{21}^2$
$\bar{\psi}\bar{\chi}\bar{\chi}$	<b>(<math>\bar{5}</math>, 35)</b>	<b>(5, 14)</b>	$\mathcal{B}_{14}^3$
		<b>+(5, 21)</b>	$\mathcal{B}_{21}^3$
	<b>(<math>\bar{5}</math>, 1)</b>	<b>(5, 1)</b>	$\mathcal{B}_1^3$

$$14 \rightarrow 8_0 + \mathbf{3}_{-2x} + \bar{\mathbf{3}}_{2x}$$

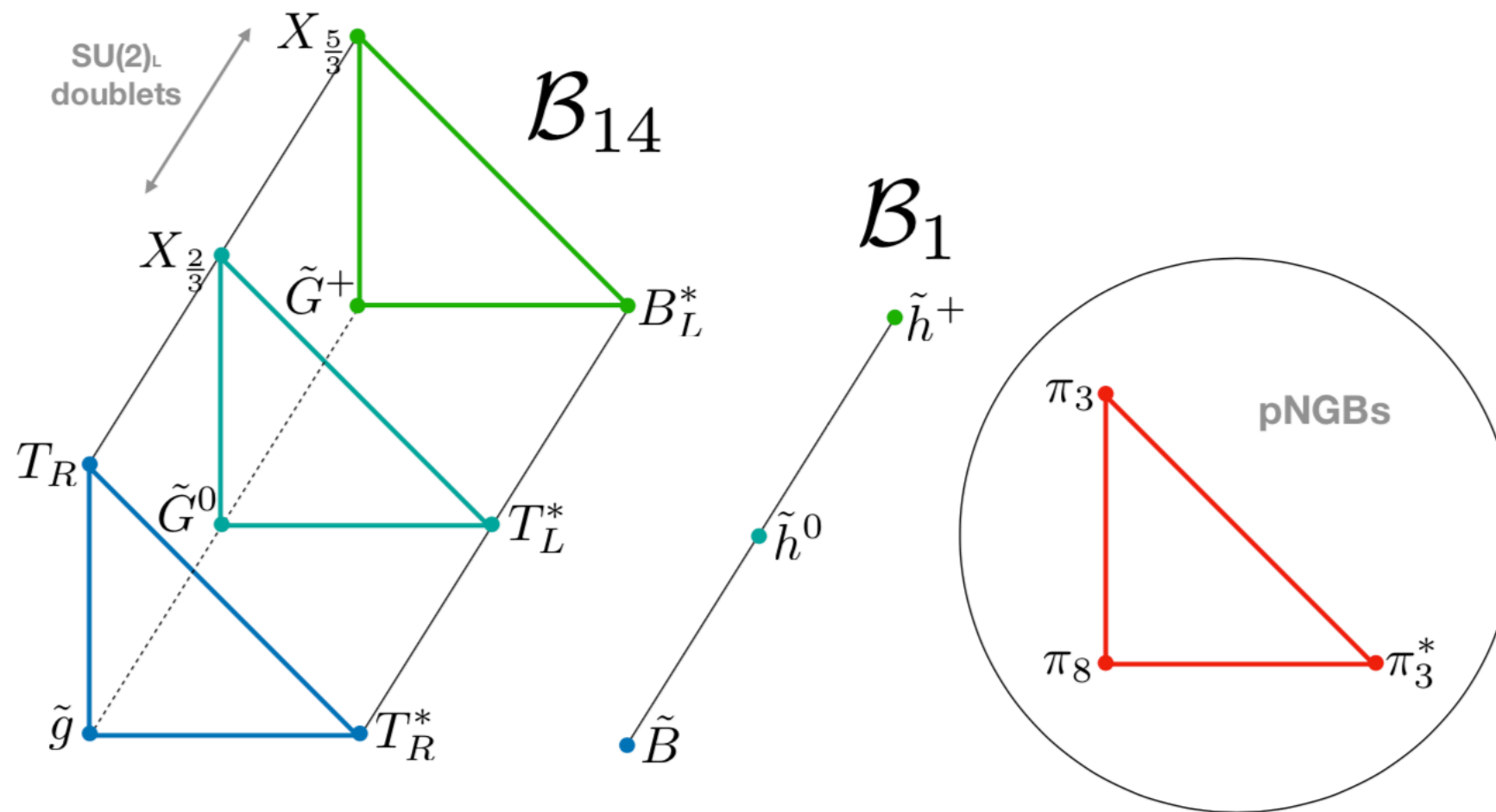
$$21 \rightarrow 8_0 + 6_{2x} + \bar{6}_{-2x} + 1_0$$



# Exotic top partners

G.C., T.Flacke, M.Kunkel, W.Porod

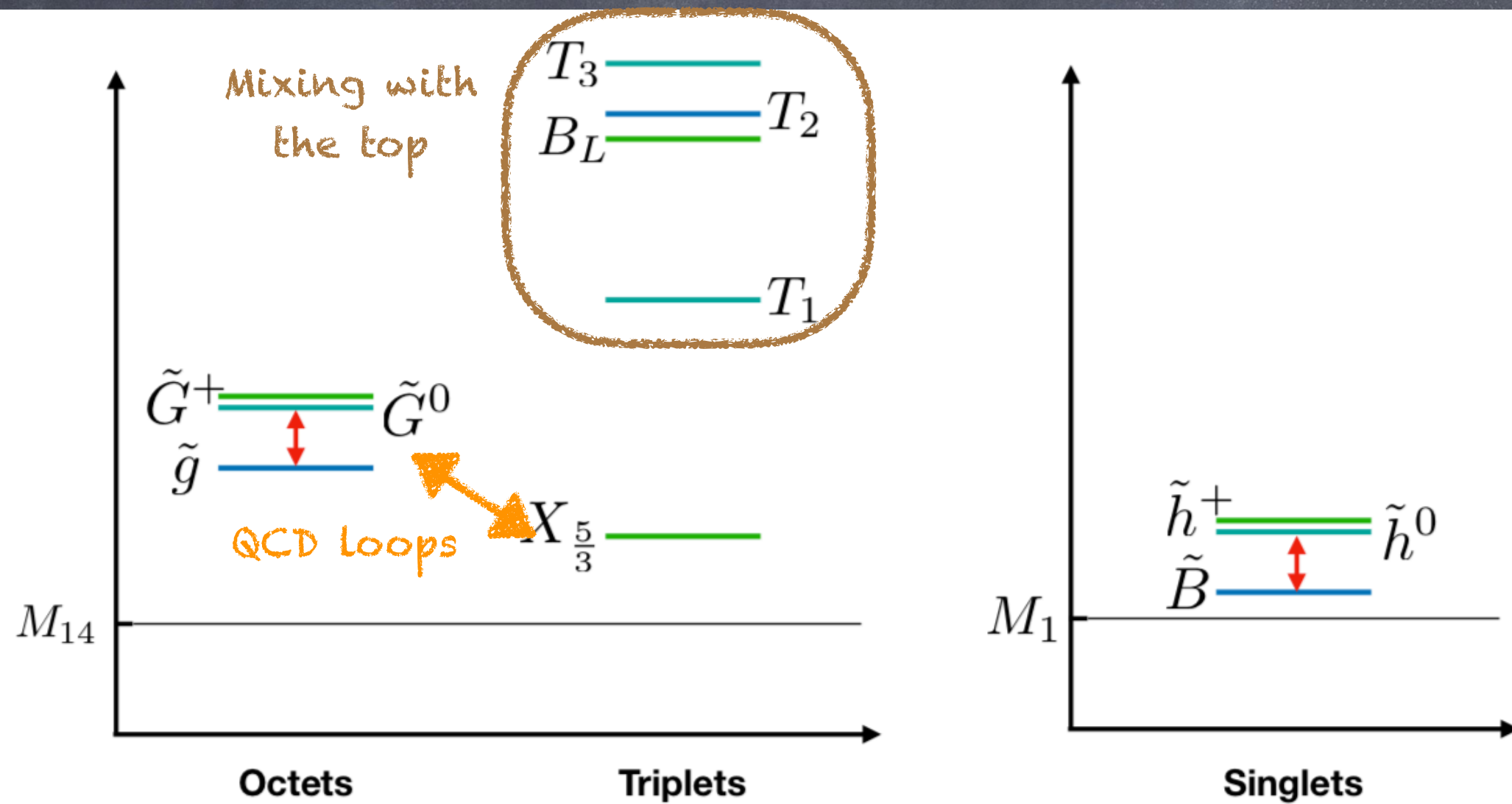
2112.00019





# Exotic top partners

G.Cacciapaglia et al.  
2112.00019



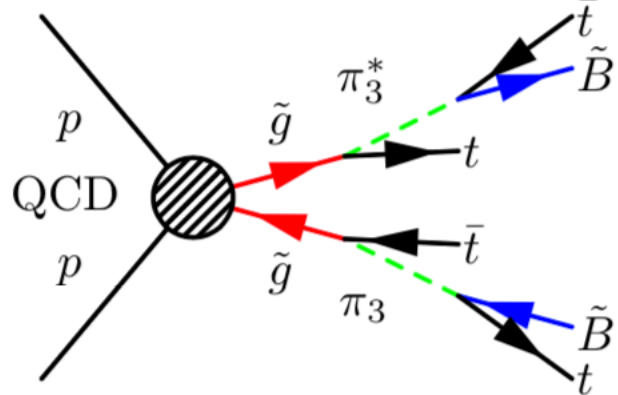


# Octoni bounds

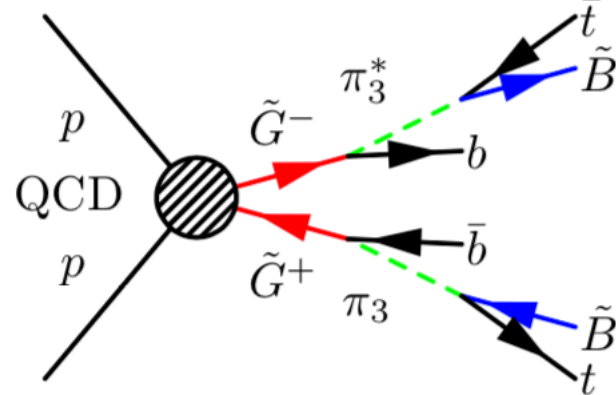
G.C., T.Flacke, M.Kunkel, W.Porod  
2112.00019

- Model implemented in MG.
- Check limits from searches in MadAnalysis and CheckMate.
- Strongest bound from gluino and stop searches!

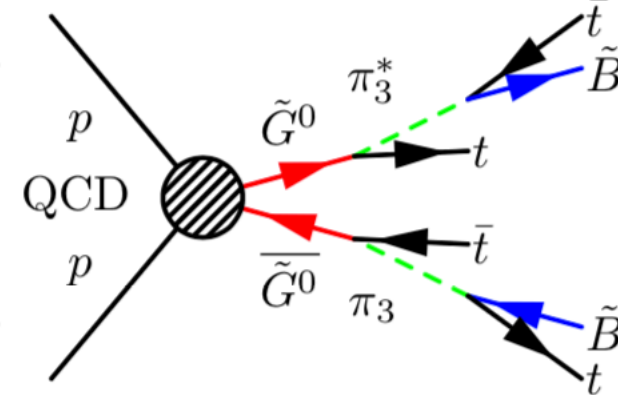




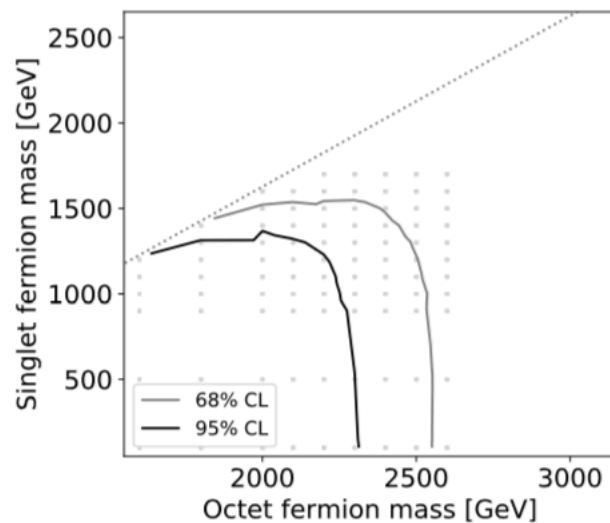
(a)  $\tilde{g} \rightarrow \bar{t}\pi_3, t\pi_3^* \rightarrow t\bar{t}\tilde{B}$



(b)  $\tilde{G}^+ \rightarrow \bar{b}\pi_3 \rightarrow \bar{b}t\tilde{B}$

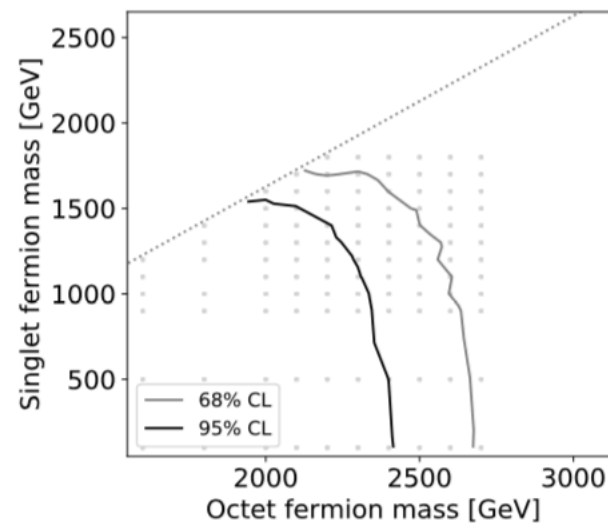


(c)  $\tilde{G}^0 \rightarrow \bar{t}\pi_3 \rightarrow t\bar{t}\tilde{B}$



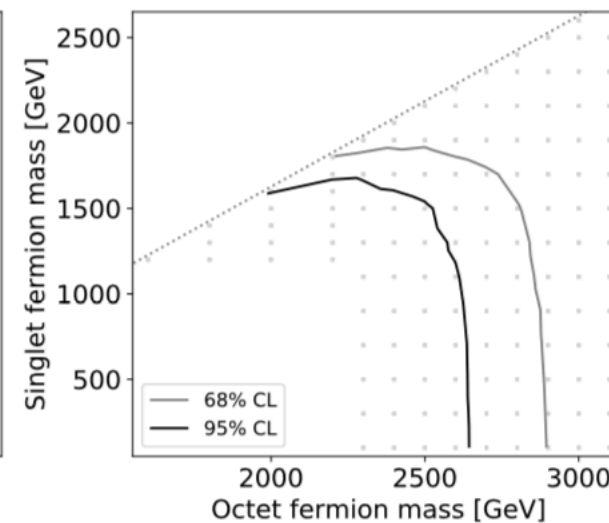
(a)  $\tilde{g} \rightarrow \bar{t}\pi_3, t\pi_3^* \rightarrow t\bar{t}\tilde{B},$

$$m_{\tilde{g}} - m_{\pi_3} = 200 \text{ GeV}$$



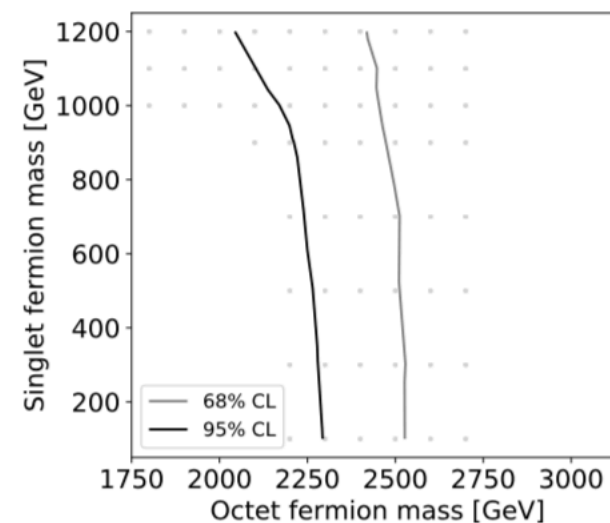
(b)  $\tilde{G}^+ \rightarrow \bar{b}\pi_3 \rightarrow \bar{b}t\tilde{B},$

$$m_{\tilde{G}^+} - m_{\pi_3} = 200 \text{ GeV}$$



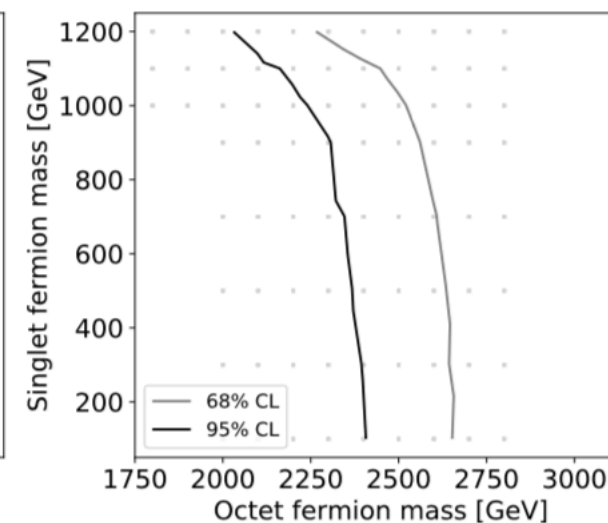
(c)  $Q_8 \rightarrow \bar{q}\pi_3 \rightarrow \bar{q}t\tilde{B},$

$$m_{Q_8} - m_{\pi_3} = 200 \text{ GeV}$$



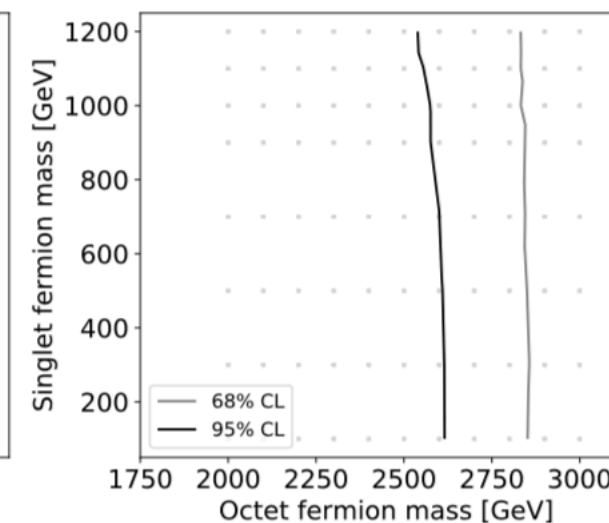
(d)  $\tilde{g} \rightarrow \bar{t}\pi_3, t\pi_3^* \rightarrow t\bar{t}\tilde{B},$

$$m_{\pi_3} = 1.4 \text{ TeV}$$



(e)  $\tilde{G}^+ \rightarrow \bar{b}\pi_3 \rightarrow \bar{b}t\tilde{B},$

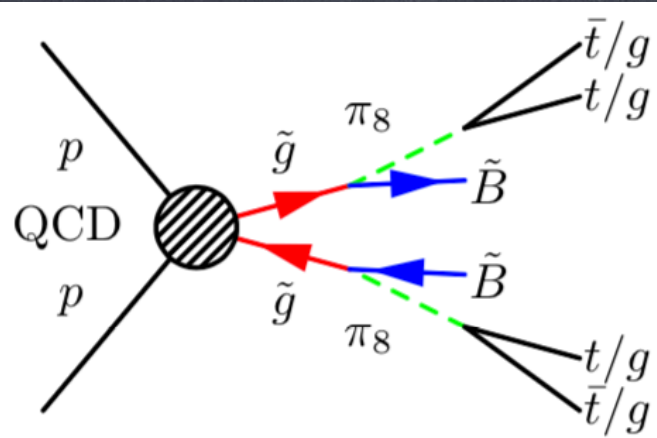
$$m_{\pi_3} = 1.4 \text{ TeV}$$



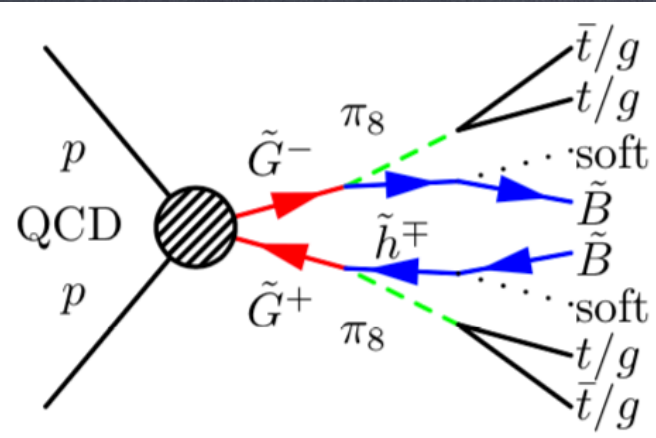
(f)  $Q_8 \rightarrow \bar{q}\pi_3 \rightarrow \bar{q}t\tilde{B},$

$$m_{\pi_3} = 1.4 \text{ TeV}$$

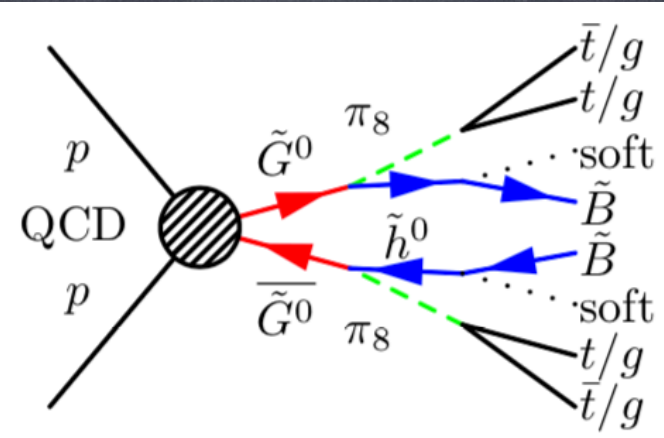




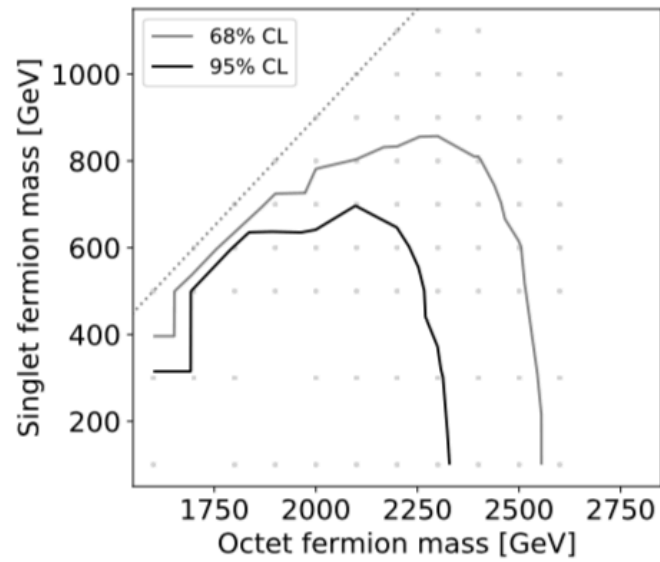
(a)  $\tilde{g} \rightarrow \tilde{B}\pi_8, \pi_8 \rightarrow \bar{t}t/gg.$



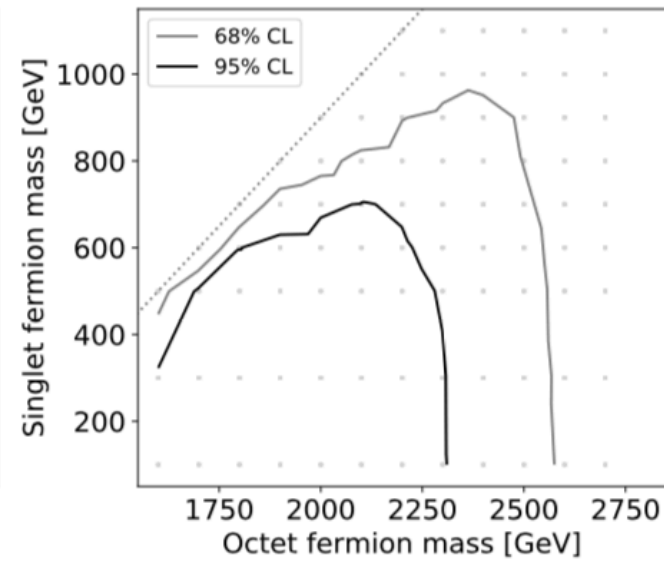
(b)  $\tilde{G}^+ \rightarrow \tilde{h}^+\pi_8, \pi_8 \rightarrow \bar{t}t/gg.$



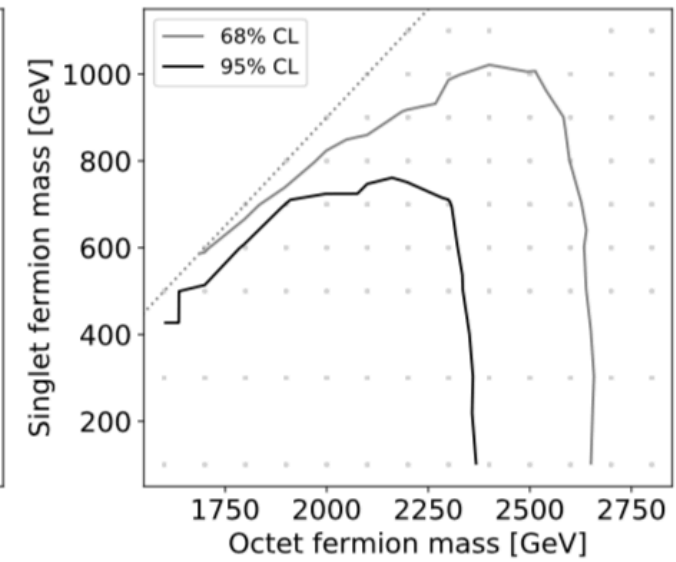
(c)  $\tilde{G}^0 \rightarrow \tilde{h}^0\pi_8, \pi_8 \rightarrow \bar{t}t/gg.$



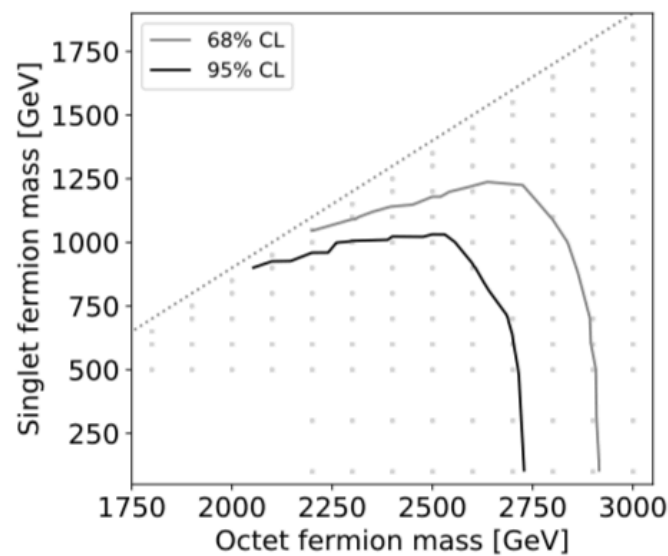
(a)  $\tilde{g} \rightarrow \pi_8\tilde{B}, \pi_8 \rightarrow gg$



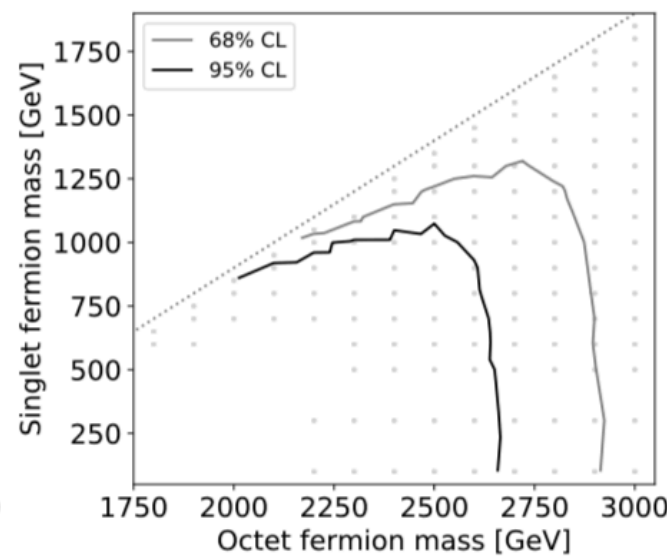
(b)  $\tilde{g} \rightarrow \pi_8\tilde{B}, \pi_8 \rightarrow gg, \bar{t}t$



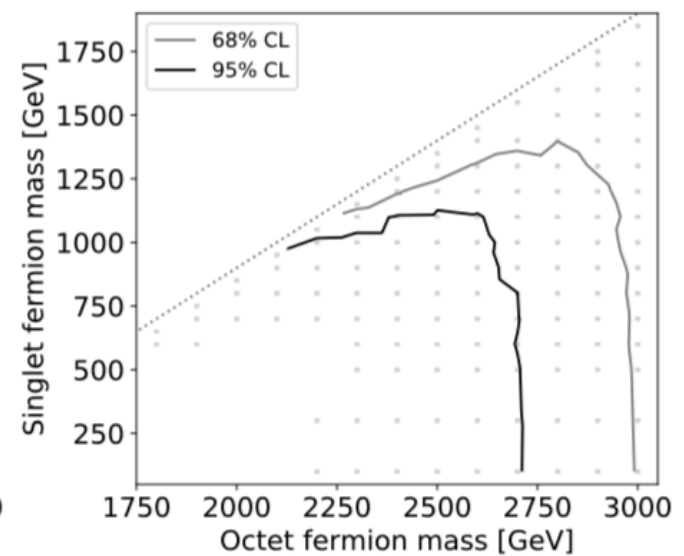
(c)  $\tilde{g} \rightarrow \pi_8\tilde{B}, \pi_8 \rightarrow \bar{t}t$



(d)  $Q_8 \rightarrow \pi_8 Q_1, \pi_8 \rightarrow gg$



(e)  $Q_8 \rightarrow \pi_8 Q_1, \pi_8 \rightarrow gg, \bar{t}t$



(f)  $Q_8 \rightarrow \pi_8 Q_1, \pi_8 \rightarrow \bar{t}t$



# Spin-1 resonances

G.C., A.Cornell, A.Deandrea, M.Kunkel, W.Porod  
2404.02198

	Models	$\chi (R, Y, B)$	$\pi$	$\mathcal{V}^\mu$	$\mathcal{A}^\mu$	$\Psi$	di-quark
C1	M1-2	$(R, -\frac{1}{3}, \frac{1}{6})$	$8_0, \mathbf{6}_{-2/3}$	$8_0, 1_0, \mathbf{3}_{2/3}$	$8_0, \mathbf{6}_{-2/3}$	$8, 1, \mathbf{3}, \mathbf{6}$	none
C2	M3-4, M8-11	$(R, \frac{2}{3}, \frac{1}{3})$	$8_0, \mathbf{6}_{4/3}$	$8_0, 1_0, \mathbf{3}_{-4/3}$	$8_0, \mathbf{6}_{4/3}$	$\mathbf{3}$	$\pi_6, \mathcal{V}_3^\mu, \mathcal{A}_6^\mu$
C3	M5	$(Pr, -\frac{1}{3}, \frac{1}{6})$	$8_0, \mathbf{3}_{2/3}$	$8_0, 1_0, \mathbf{6}_{-2/3}$	$8_0, \mathbf{3}_{2/3}$	$8, 1, \mathbf{3}, \mathbf{6}$	none
C4	M6-7	$(C, -\frac{1}{3}, \frac{1}{6})$	$8_0$	$8_0, 1_0$	$8_0$	$8, 1, \mathbf{3}, \mathbf{6}$	none
C5	M12	$(C, \frac{2}{3}, \frac{1}{3})$	$8_0$	$8_0, 1_0$	$8_0$	$\mathbf{3}$	none

- Octets (and one singlet) ubiquitous
- $V_8$  always mixes with the gluon ( $V_1$  with hypercharge)
- Triplets and sextets present in C1, C2 and C3.



# Spin-1 resonances: decays

G.C., A.Cornell, A.Deandrea, M.Kunkel, W.Porod  
2404.02198

- Couplings to pNGBs

$$\mathcal{O}_V = i \text{Tr}([\pi, \partial_\mu \pi] V^\mu),$$

$$\mathcal{O}_A = \text{Tr}([\pi, [\pi, \partial_\mu \pi]] A^\mu),$$

$$V \rightarrow \pi\pi$$

$$A \rightarrow \pi\pi\pi$$

Determined by  $g_{\rho\pi\pi}$

- Octet couplings to quarks via mixing

Determined by  $\tilde{g}$

- Couplings to tops via Partial Compositeness



Determined by  $g_{\rho BB}$



# Spin-1 resonances: decays

G.C., A.Cornell, A.Deandrea, M.Kunkel, W.Porod  
2404.02198

## • Couplings to pNGBs

$$\mathcal{O}_V = i \text{Tr}([\pi, \partial_\mu \pi] V^\mu),$$

$$\mathcal{O}_A = \text{Tr}([\pi, [\pi, \partial_\mu \pi]] A^\mu)$$

$$V \rightarrow \pi\pi$$

Determined by  $g_{\rho\pi\pi}$

## • Oct

$$\text{C1-2 : } \mathcal{V}_8 \rightarrow qq\bar{q}, bb\bar{b}, tt\bar{t}, \pi_8\pi_8, \pi_6\pi_6^c,$$

$$\text{C3 : } \mathcal{V}_8 \rightarrow qq\bar{q}, bb\bar{b}, tt\bar{t}, \pi_8\pi_8, \pi_3\pi_3^c,$$

$$\text{C4-5 : } \mathcal{V}_8 \rightarrow qq\bar{q}, bb\bar{b}, tt\bar{t}, \pi_8\pi_8,$$

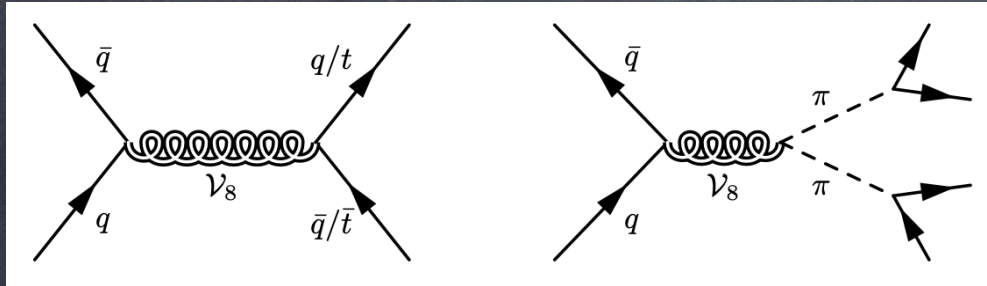
## • Couplings to tops via Partial Compositeness



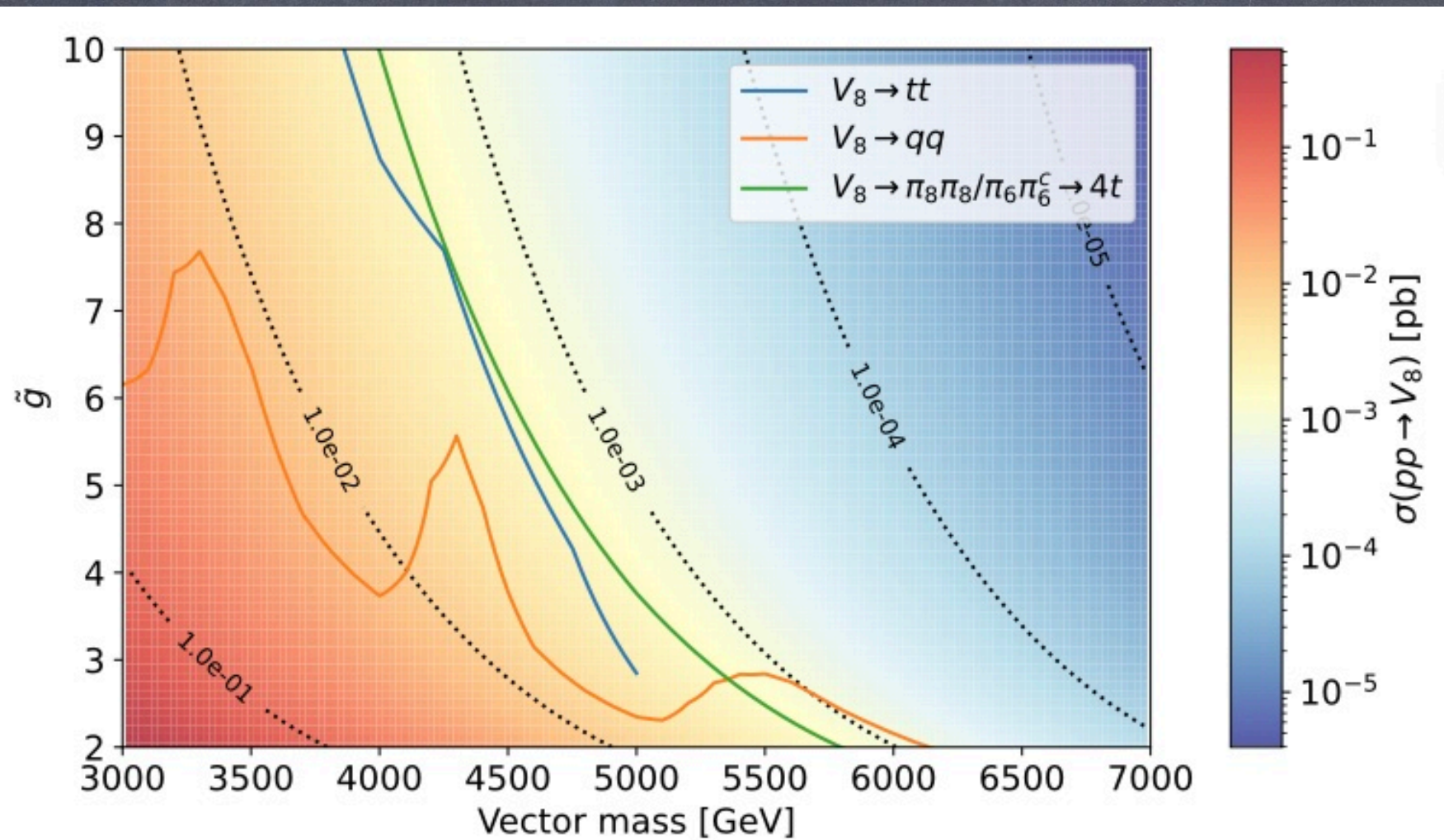
Determined by  $g_{\rho BB}$



# Spin-1 resonances: LHC bounds



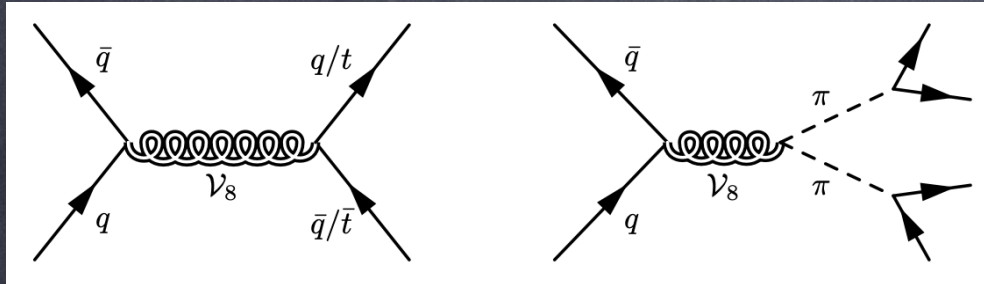
G.C., A.Cornell, A.Deandrea, M.Kunkel, W.Porod  
2404.02198



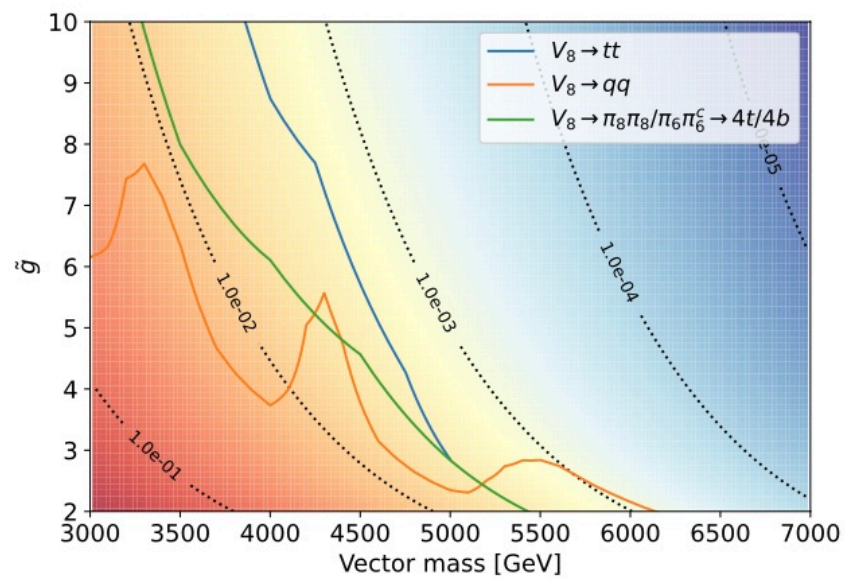
(b) Class C2



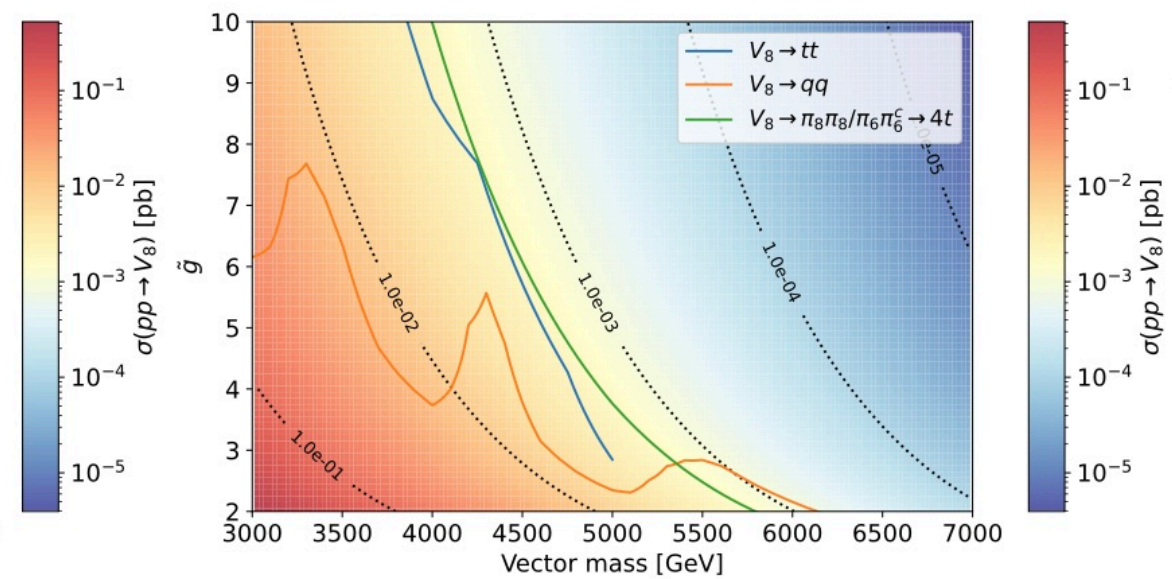
# Spin-1 resonances: LHC bounds



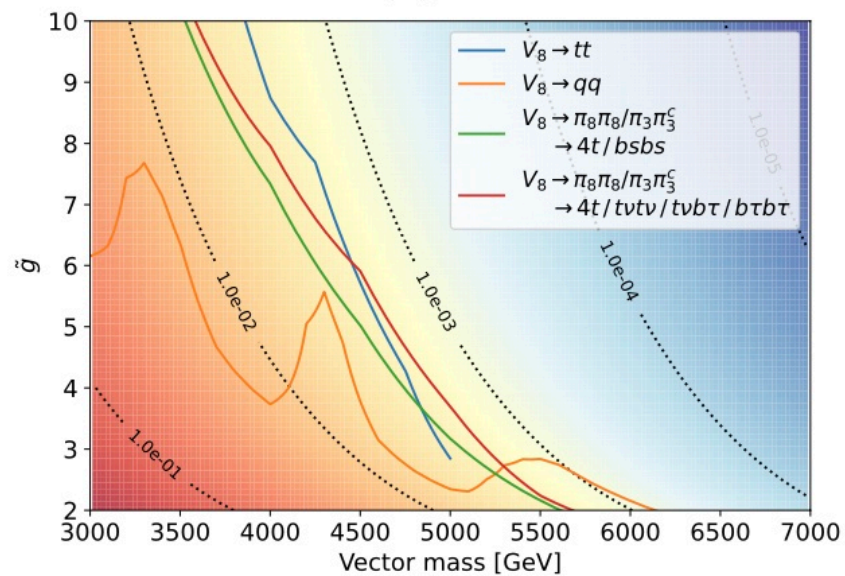
G.C., A.Cornell, A.Deandrea, M.Kunkel, W.Porod  
2404.02198



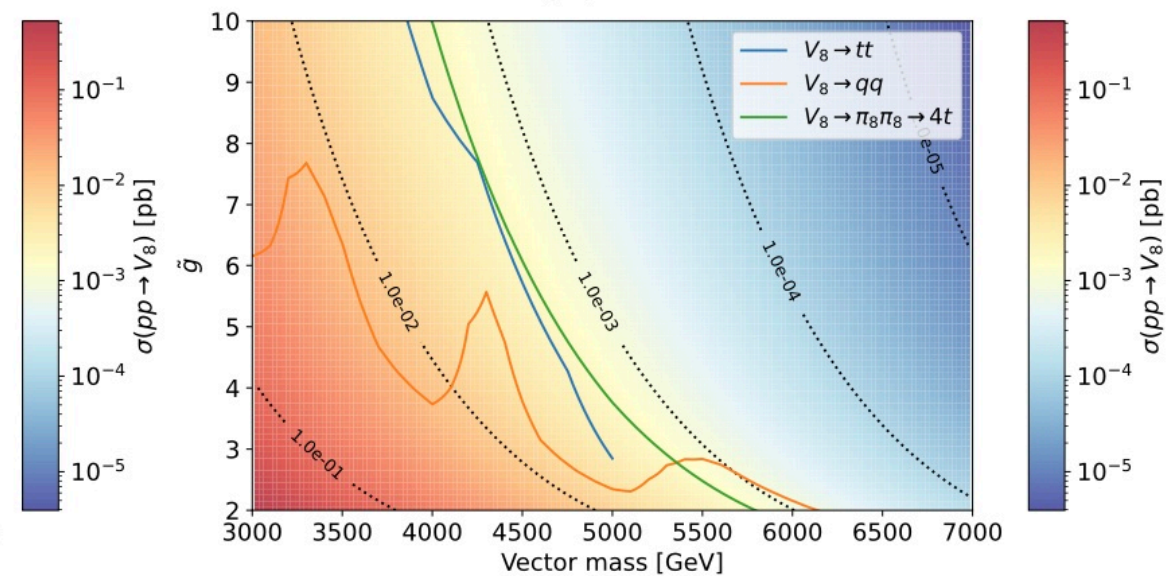
(a) Class C1



(b) Class C2



(c) Class C3



(d) Classes C4-5



# The FCC-ee\* legacy

(\* aka CEPC, ILC, ...)

- The Higgs (precision)
- EW precision tests
- Light singlets (ALPs) below the Z mass



# Typical ALP Lagrangian:

$$\mathcal{L}_{\text{eff}}^{D \leq 5} = \frac{1}{2} (\partial_\mu a)(\partial^\mu a) - \frac{m_{a,0}^2}{2} a^2 + \frac{\partial^\mu a}{\Lambda} \sum_F \bar{\psi}_F \mathbf{C}_F \gamma_\mu \psi_F$$

$$+ g_s^2 C_{GG} \frac{a}{\Lambda} G_{\mu\nu}^A \tilde{G}^{\mu\nu,A} + g^2 C_{WW} \frac{a}{\Lambda} W_{\mu\nu}^A \tilde{W}^{\mu\nu,A} + g'^2 C_{BB} \frac{a}{\Lambda} B_{\mu\nu} \tilde{B}^{\mu\nu},$$

Composite Higgs scenario:

$$\frac{C_{WW}}{\Lambda} \sim \frac{C_{BB}}{\Lambda} \sim \frac{N_{\text{TC}}}{64\sqrt{2} \pi^2 f}$$

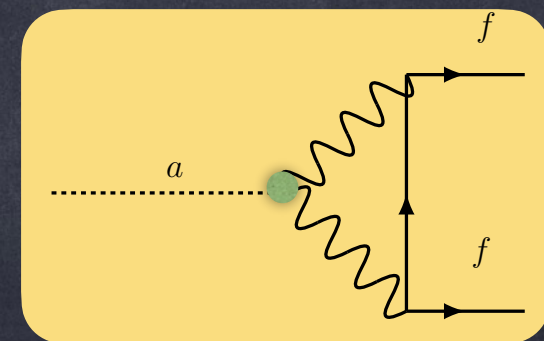
$$\frac{C_{GG}}{\Lambda} = 0$$

(Poor bounds at the LHC)

$$(C_{\gamma\gamma} = C_{WW} + C_{BB})$$

$\mathbf{C}_F$  is loop-induced:

M.Bauer et al, 1708.00443





# Typical ALP Lagrangian:

$$\mathcal{L}_{\text{eff}}^{D \leq 5} = \frac{1}{2} (\partial_\mu a)(\partial^\mu a) - \frac{m_{a,0}^2}{2} a^2 + \frac{\partial^\mu a}{\Lambda} \sum_F \bar{\psi}_F \mathbf{C}_F \gamma_\mu \psi_F \\ + g_s^2 C_{GG} \frac{a}{\Lambda} G_{\mu\nu}^A \tilde{G}^{\mu\nu,A} + g^2 C_{WW} \frac{a}{\Lambda} W_{\mu\nu}^A \tilde{W}^{\mu\nu,A} + g'^2 C_{BB} \frac{a}{\Lambda} B_{\mu\nu} \tilde{B}^{\mu\nu},$$


Composite Higgs scenario:

$$\frac{C_{WW}}{\Lambda} \sim \frac{C_{BB}}{\Lambda} \sim \frac{N_{\text{TC}}}{64\sqrt{2} \pi^2 f}$$

Free parameters:

$$(C_{\gamma\gamma} = C_{WW} + C_{BB})$$

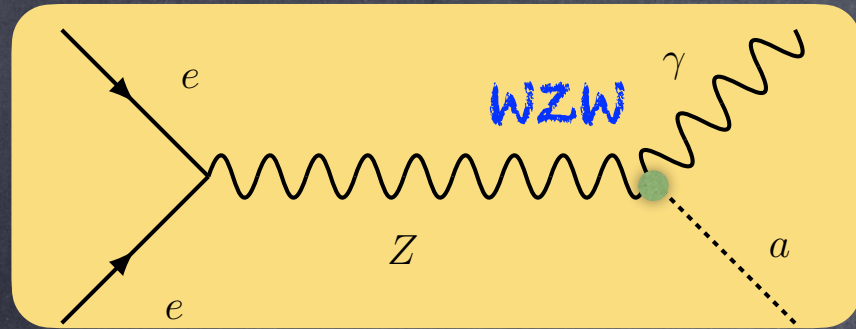
We will consider two scenarios:  
Photo-philic and  
Photo-phobic



$f, m_a$



# Tera-Z portal to compositeness (via ALPs)

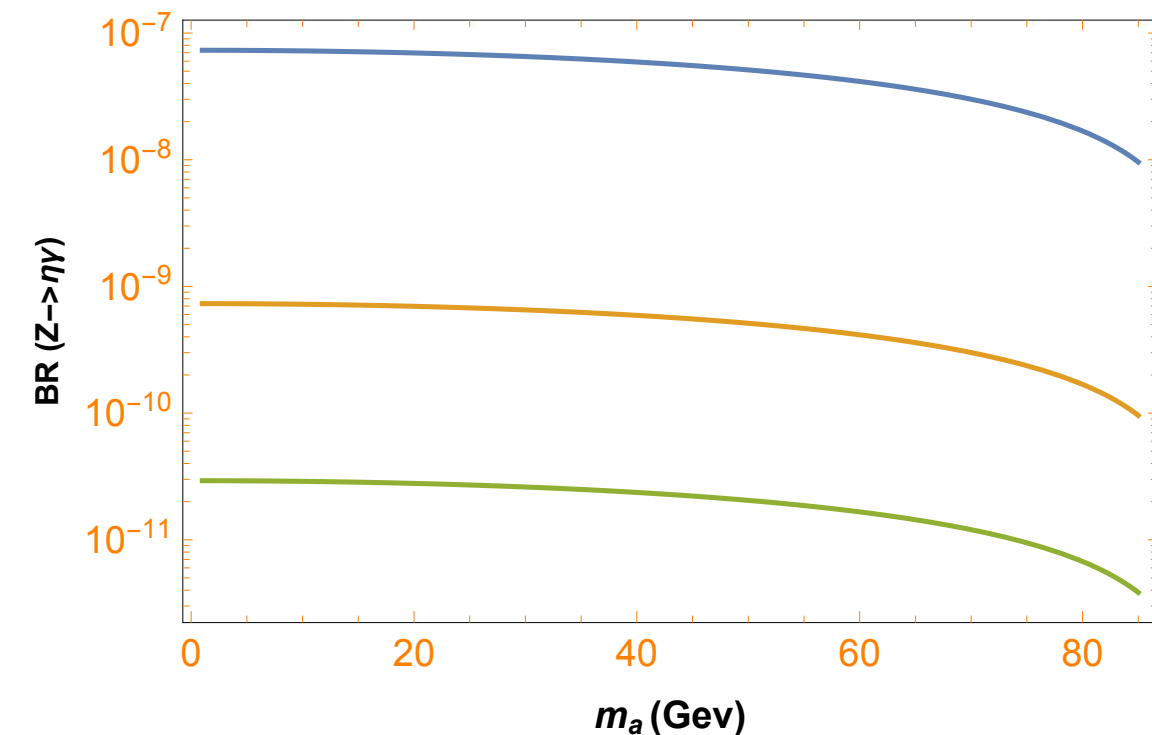


G.C., A.Deandrea, A.Iyer, Sridhar  
2104.11064

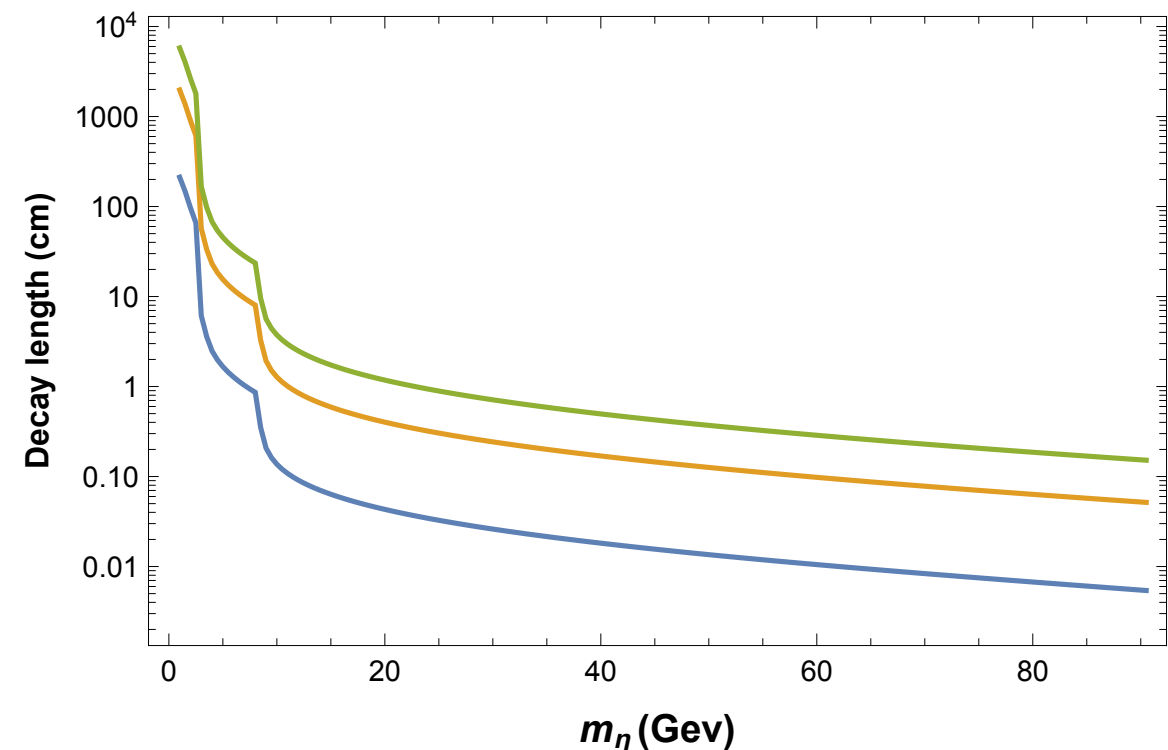
This process is always associated  
with a monochromatic photon.

Tera Z phase of FCC-ee will lead to 5-6  $10^{12}$  Z bosons  
at the end of the run.

Ideal test for rare Z decays!!



—  $f = 1$  TeV  
—  $f = 10$  TeV  
—  $f = 50$  TeV



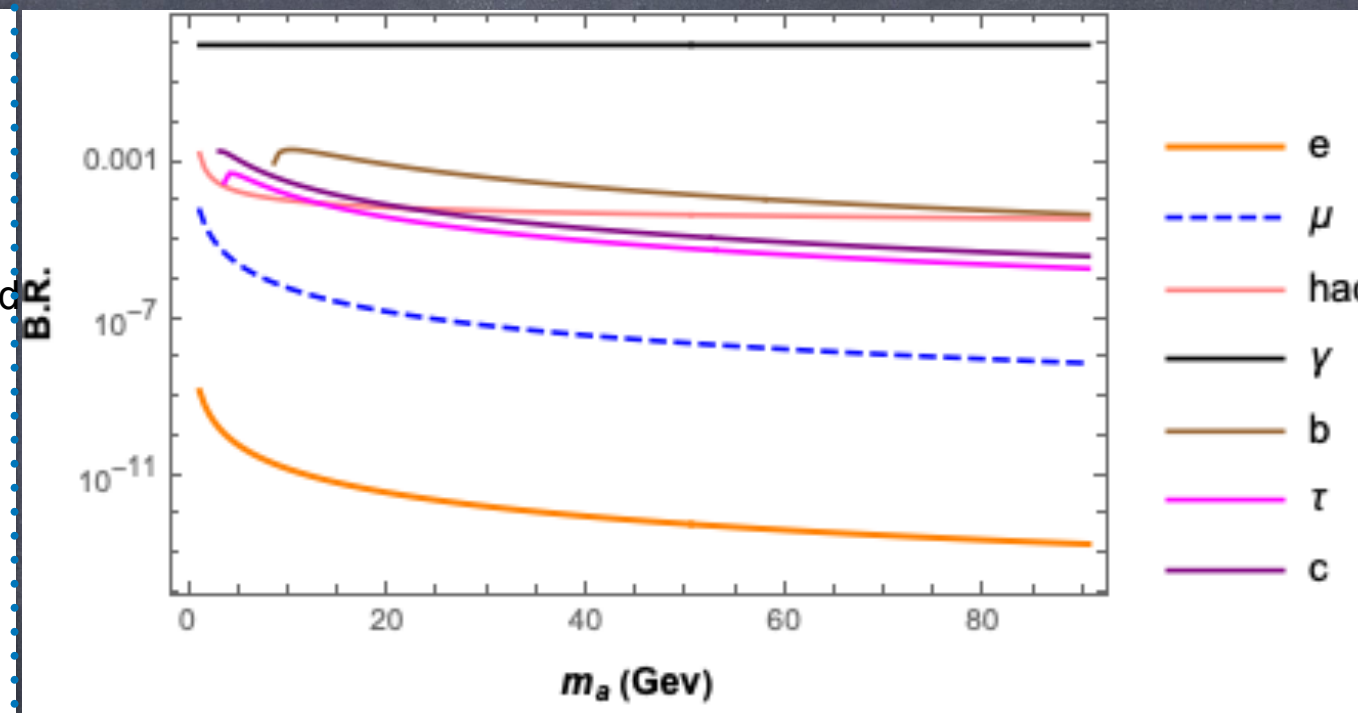
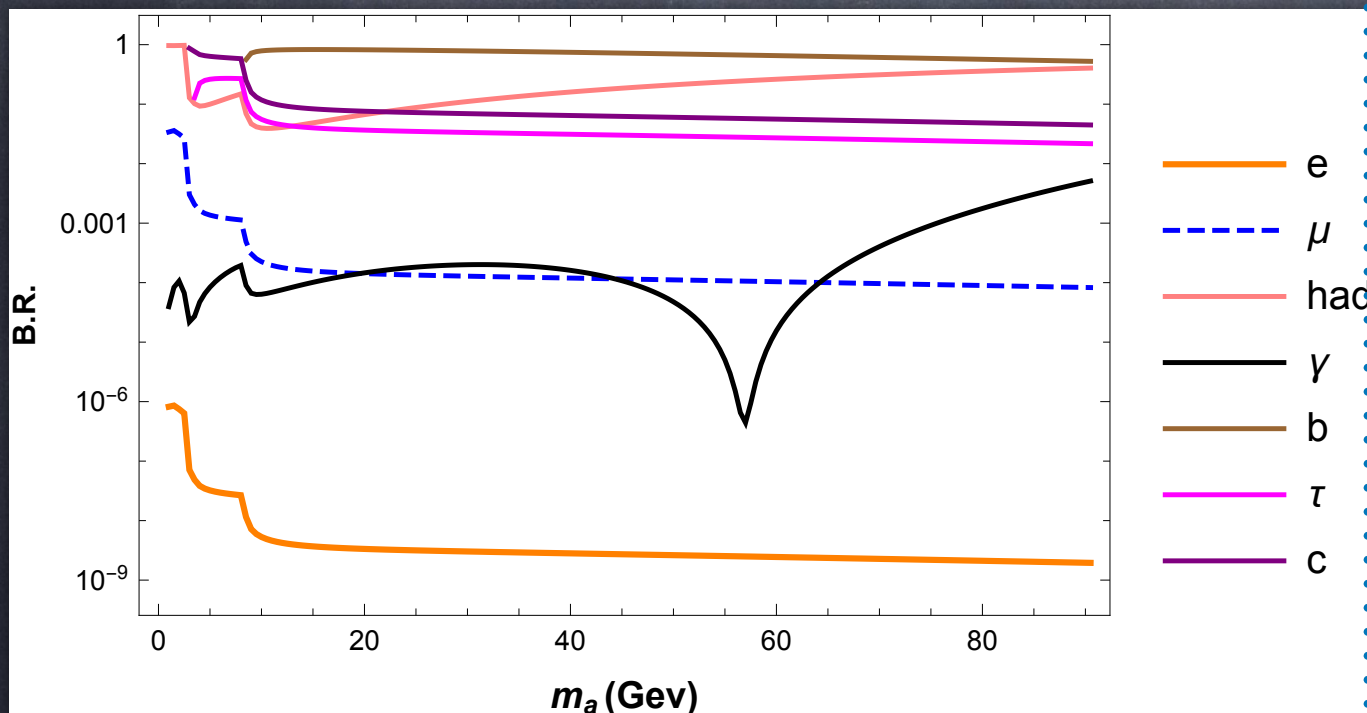


# Tera-Z portal to compositeness (via ALPs)

G.C., A.Deandrea, A.Iyer, Sridhar  
2104.11064

## Photo-phobic

## Photo-philic



No leading order coupling to  
Photons (WZW interaction is Zero!!)

eg.  $SU(4)/SP(4)$ ,  
 $SU(4) \times SU(4)/SU(4)$

WZW interaction to photons  
(Like the pion)

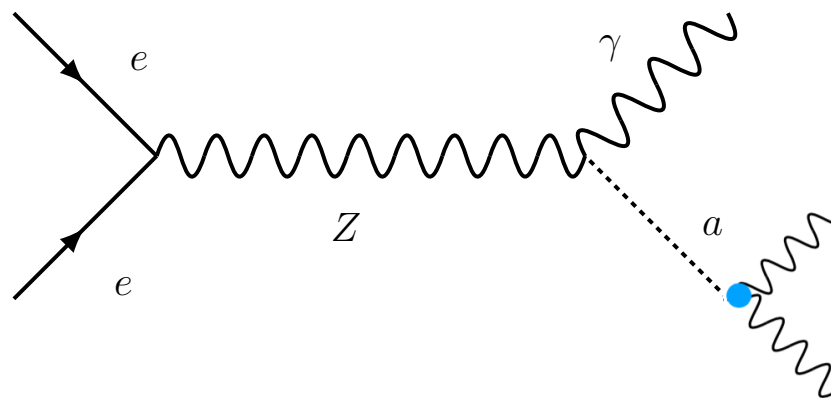
eg.  $SU(5)/SO(5)$ ,  
 $SU(6)/SO(6)$



# Phenomenology-Prompt Decays

## Photo-philic

G.C. et al.  
2104.11064



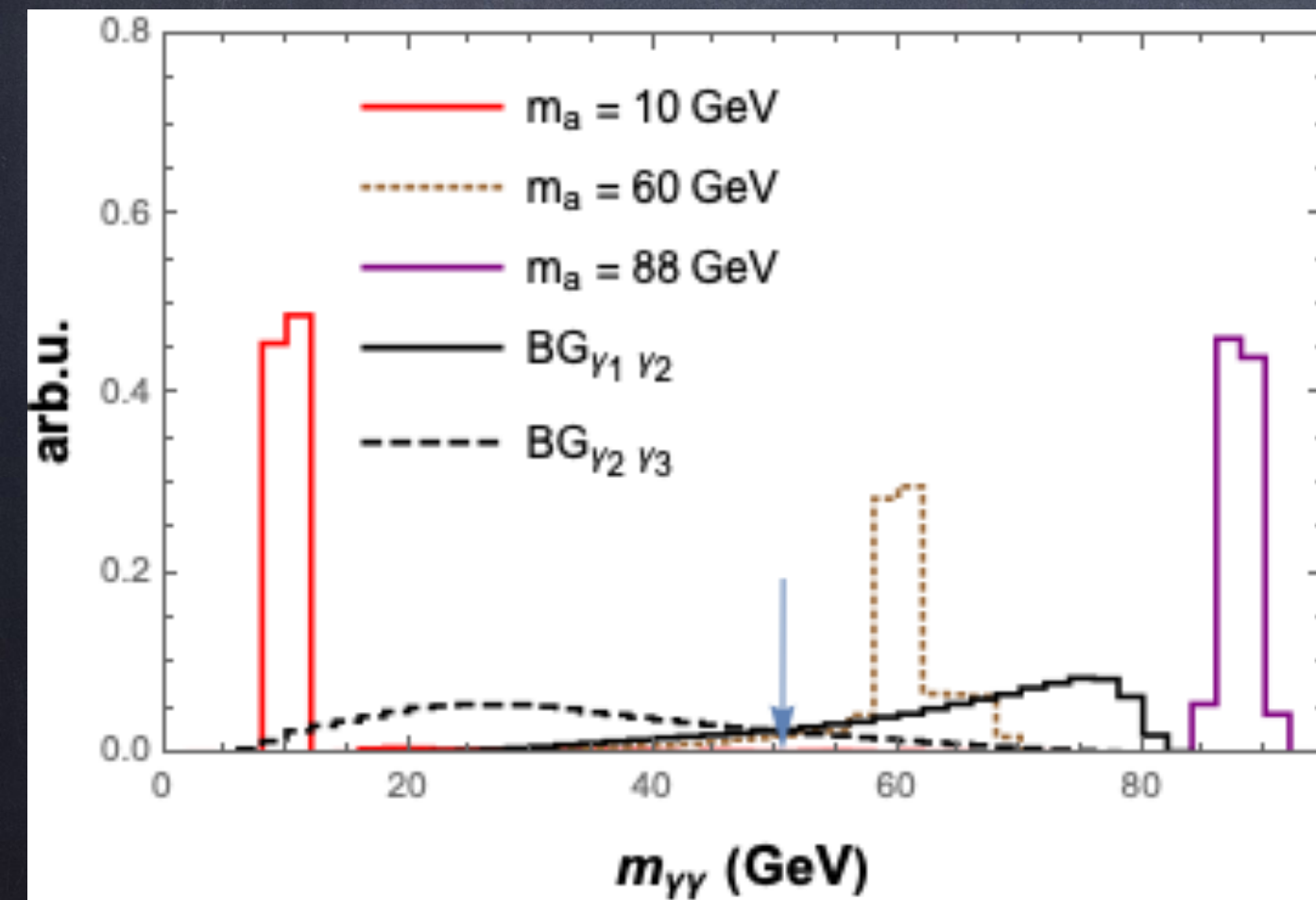
- Three isolated photons

$$BR(Z \rightarrow 3\gamma)_{\text{LEP}} < 2.2 \cdot 10^{-6}$$

Discriminating variable:  
invariant mass

Photon ordering changes  
at inv. mass 50 GeV

Bins above 80 GeV  
populated by fakes:  
hard to estimate!





# Phenomenology

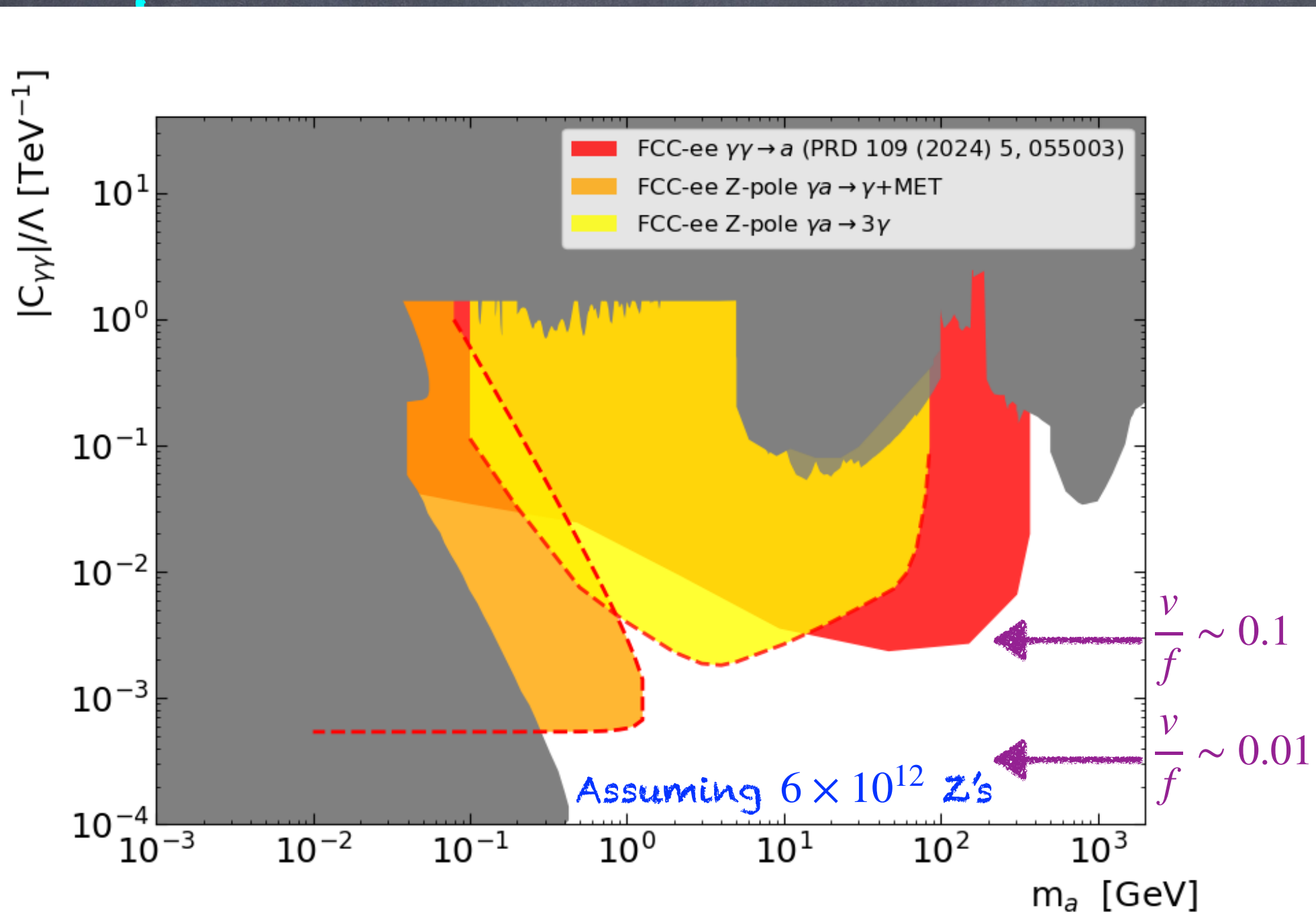
G.Polesello, 2502.08411

+ work in progress

Two searches:

- prompt decays to photons;
- Decay outside the detector.

## Photo-philic





# What if FCC-ee discovers $Z \rightarrow \gamma a$ ?

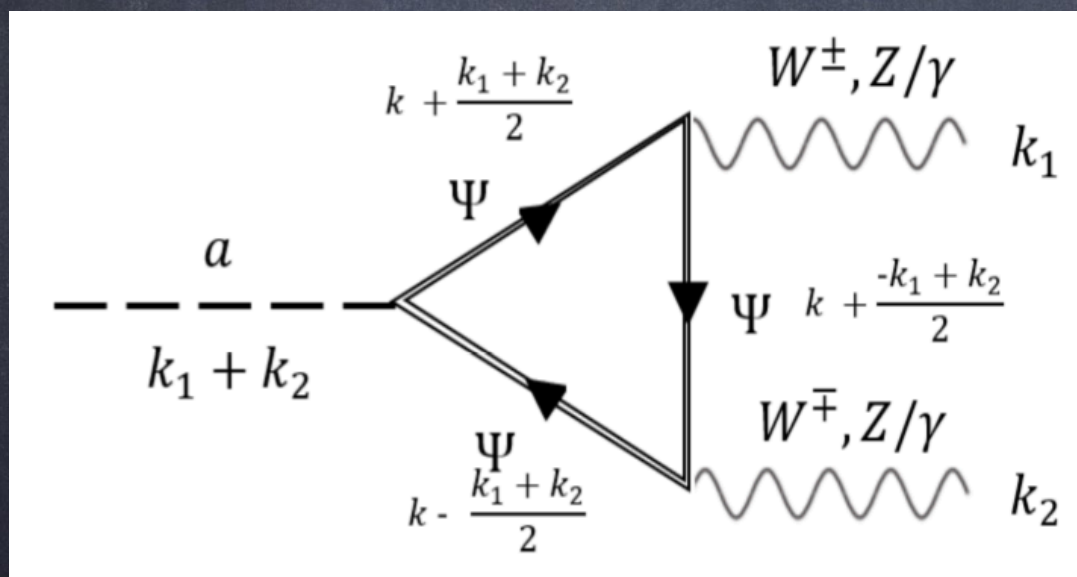
G.C., A.Deandrea, A.Iyer, A.Pinto  
2211.00961

- Is it possible to distinguish the composite scenario, from an elementary mock-up model?

$$\Phi = H + i a$$

Singlet scalar

$$\Psi = \text{doublet} + \text{singlet}$$



Triangle loops can mimic the WZW interactions of the composite ALP:

doublet + singlet =  
photo-phobic case

- Note: fermion masses of the order of TeV, potentially discoverable at HL-LHC or FCC-hh (QCD-neutral)

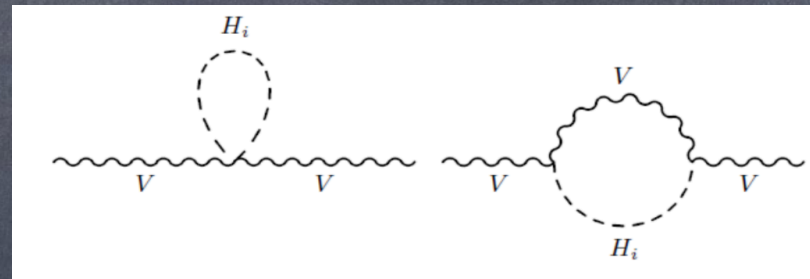


# What if FCC-ee discovers $Z \rightarrow \gamma a$ ?

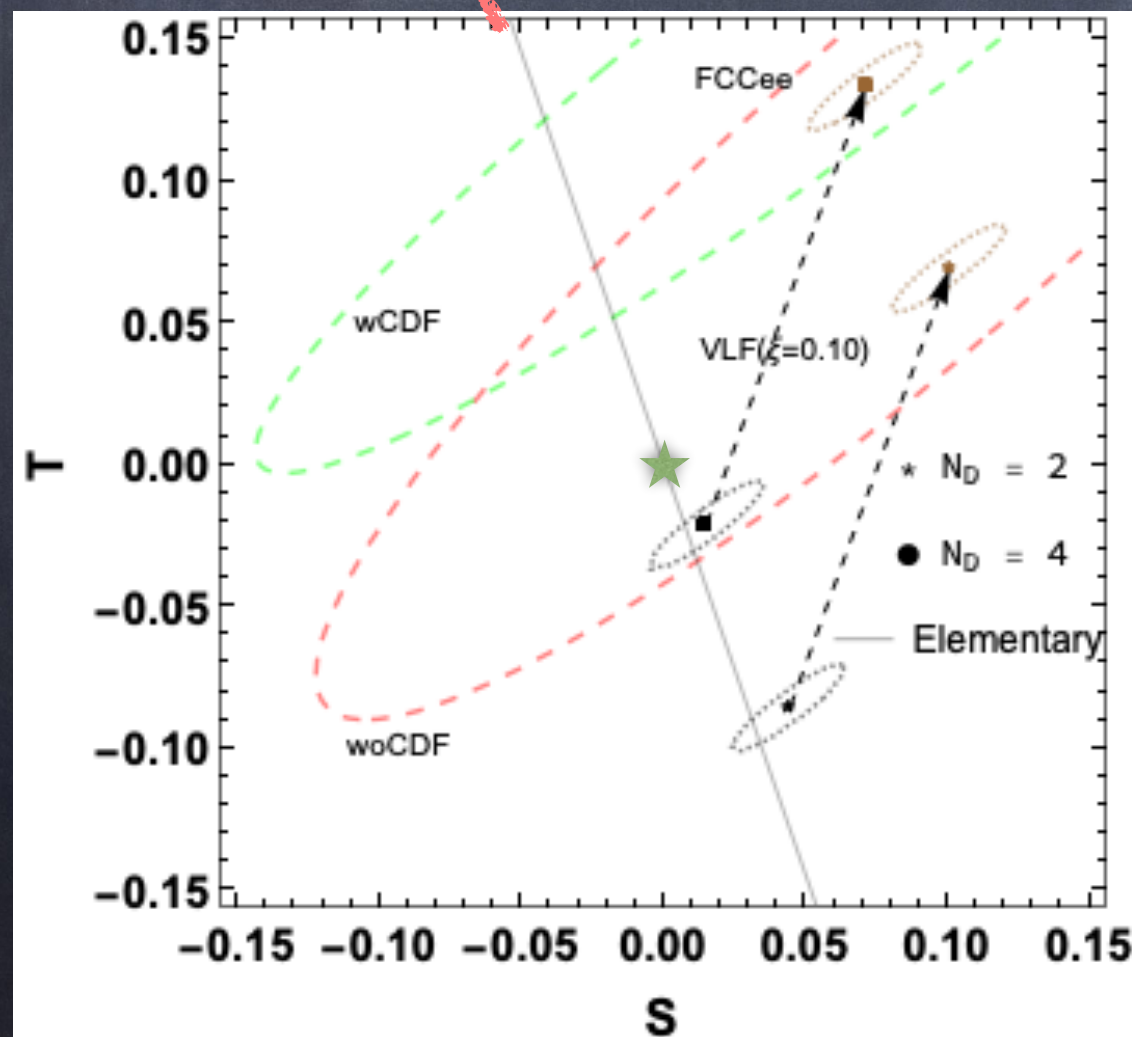
G.C., A.Deandrea, A.Iyer, A.Pinto  
2211.00961

- Is it possible to distinguish the composite scenario, from an elementary mock-up model?

EWPT only depend  
on  $H$  loops



composite case:  
see 1502.04718



For fixed  $BR = 10^{-8}$ ,  
i.e. discovery.

Arrows: naive contribution  
of top partner loops.



# The FCC-hh\* legacy

(\* aka CEPC, ILC, ...)

- The Higgs potential (trilinear)
- Heavy resonances
- Multi-boson production (precursors of techni-jets)



# Spin-1 resonances: FCC-hh

G.C., A.Cornell, A.Deandrea, M.Kunkel, W.Porod  
2404.02198

- Pair production becomes relevant
- Dominant channel is the sextet (when present)
- Note: the octet should be discovered in single production channel!

$$\mathcal{V}_6 \rightarrow \pi_8 \pi_3^\dagger \rightarrow (t\bar{t})(\bar{b}s \text{ or } ql) \quad \text{in C3}$$

$$\mathcal{A}_6 \rightarrow \pi_8 \pi_8 \pi_6 (t\bar{t}t\bar{t}bb) \text{ and } \pi_6^\dagger \pi_6 \pi_6 (\bar{b}\bar{b}bbbb) \quad \text{in C1}$$

$$\mathcal{A}_6 \rightarrow t\bar{t} \text{ or } \pi_8 \pi_8 \pi_6 (t\bar{t}t\bar{t}t\bar{t}) \text{ and } \pi_6^\dagger \pi_6 \pi_6 (\bar{t}\bar{t}t\bar{t}t\bar{t}) \quad \text{in C2}$$



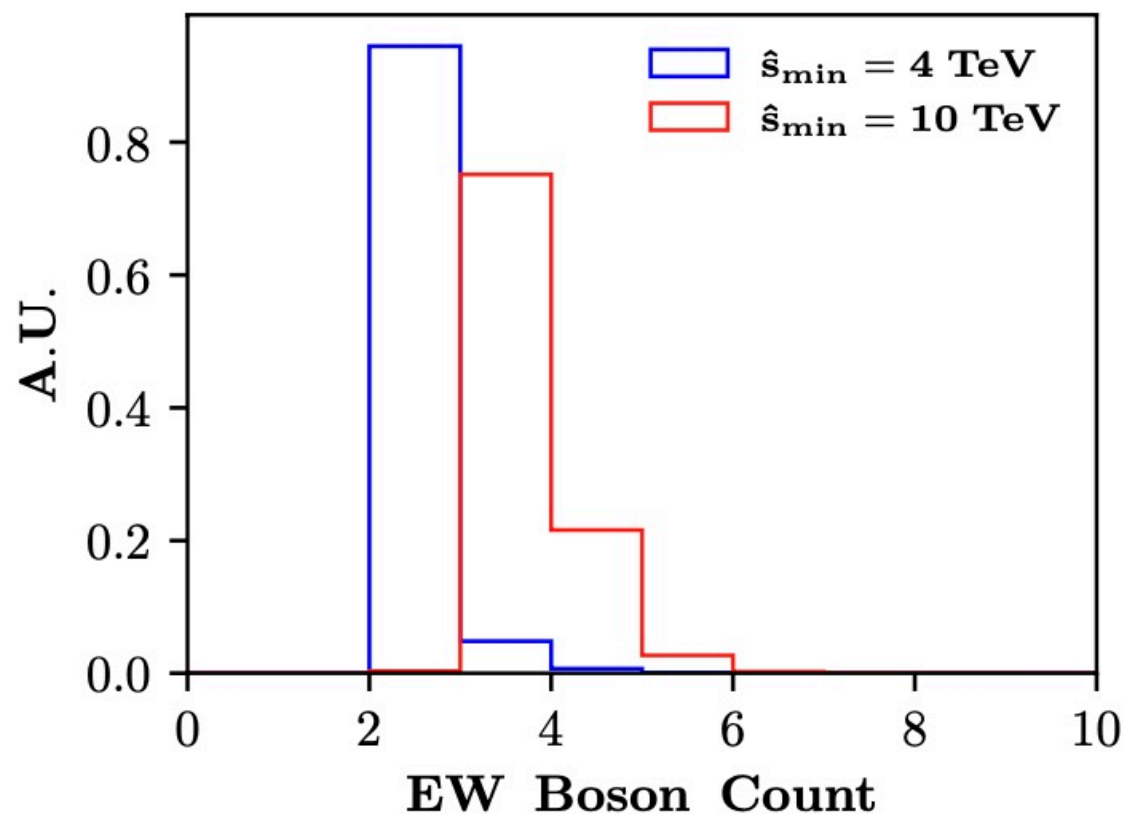
# Multi-boson production

G.C., A.Deandrea, A.Iyer, S.Kulkarni, A.Singh  
Work in progress

- Study high-energy multi-boson production via techni-quark Drell-Yan

We simulated events with  
 $m_Q = \Lambda_{TC} = 2 \text{ TeV}$

Multiboson dominant  
at large energies



$\hat{s}_{\min}$ (TeV)	3 Bosons		4 Bosons	
	$\sigma_{SM}$ (ab)	$\sigma_{sig}$ (ab)	$\sigma_{SM}$ (ab)	$\sigma_{sig}$ (ab)
10	685.18	122.03	140.88	33.54
20	23.30	0.1542	6.49	0.2052
30	1.41	0.0014	0.47	0.0015



# The composite Higgs Roadmap

- LHC: Higgs, EW scalars, coloured states
- FCC-ee: EW precision + Higgs, Light ALPs  $\rightarrow$  Indications on the compositeness scale and top partner structures
- FCC-hh: discovery up to 10 TeV, jetty structures
- Complementary programme: flavour experiments, gravitational waves (LISA), ...